

Поиск эпистаза в экспериментальных данных, полученных случайным мутагенезом

Семинар «Суперкомпьютерное моделирование в
науке и инженерии», МИЭМ НИУ ВШЭ

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Skoltech



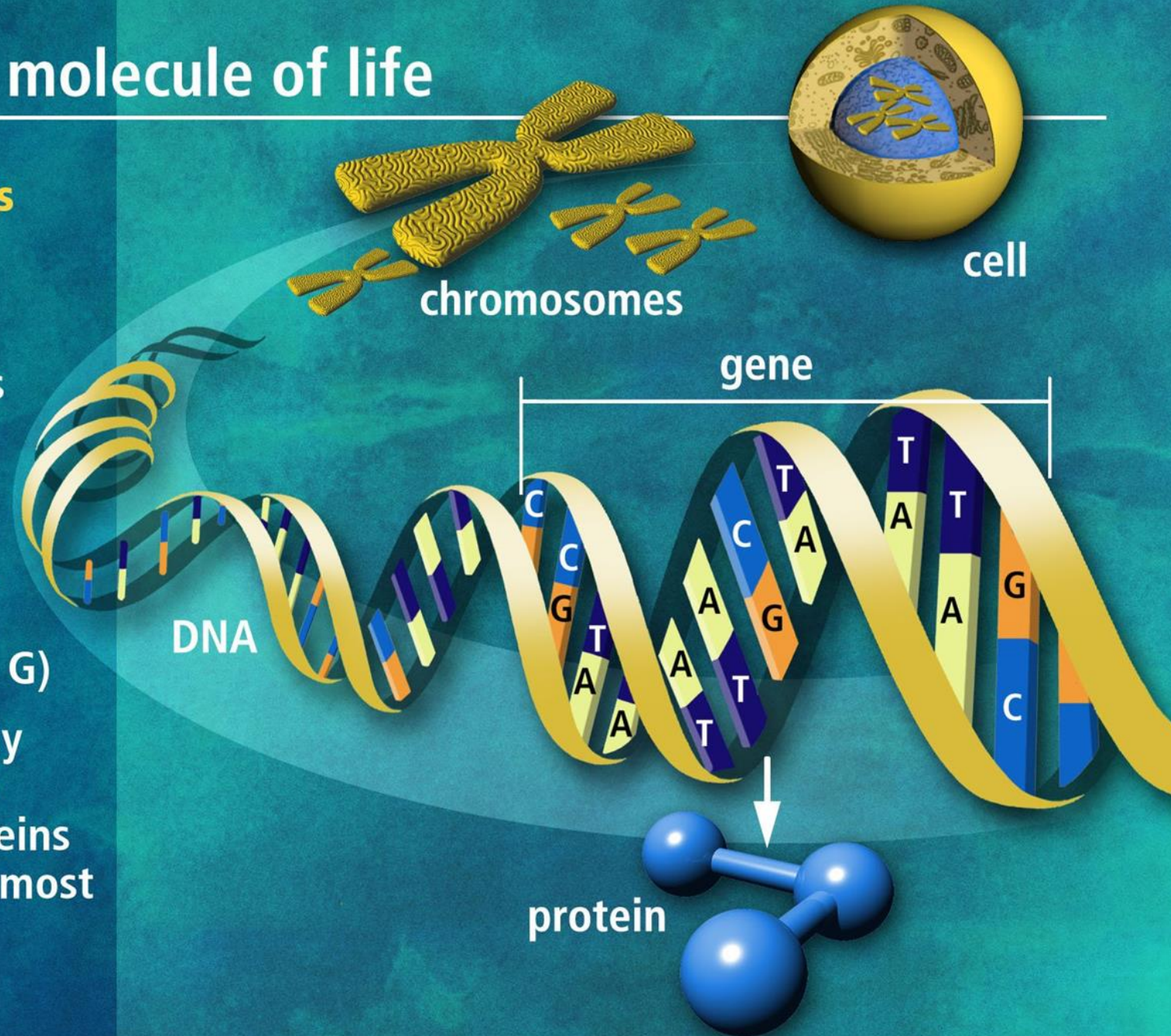
Genome

DNA the molecule of life

Trillions of cells

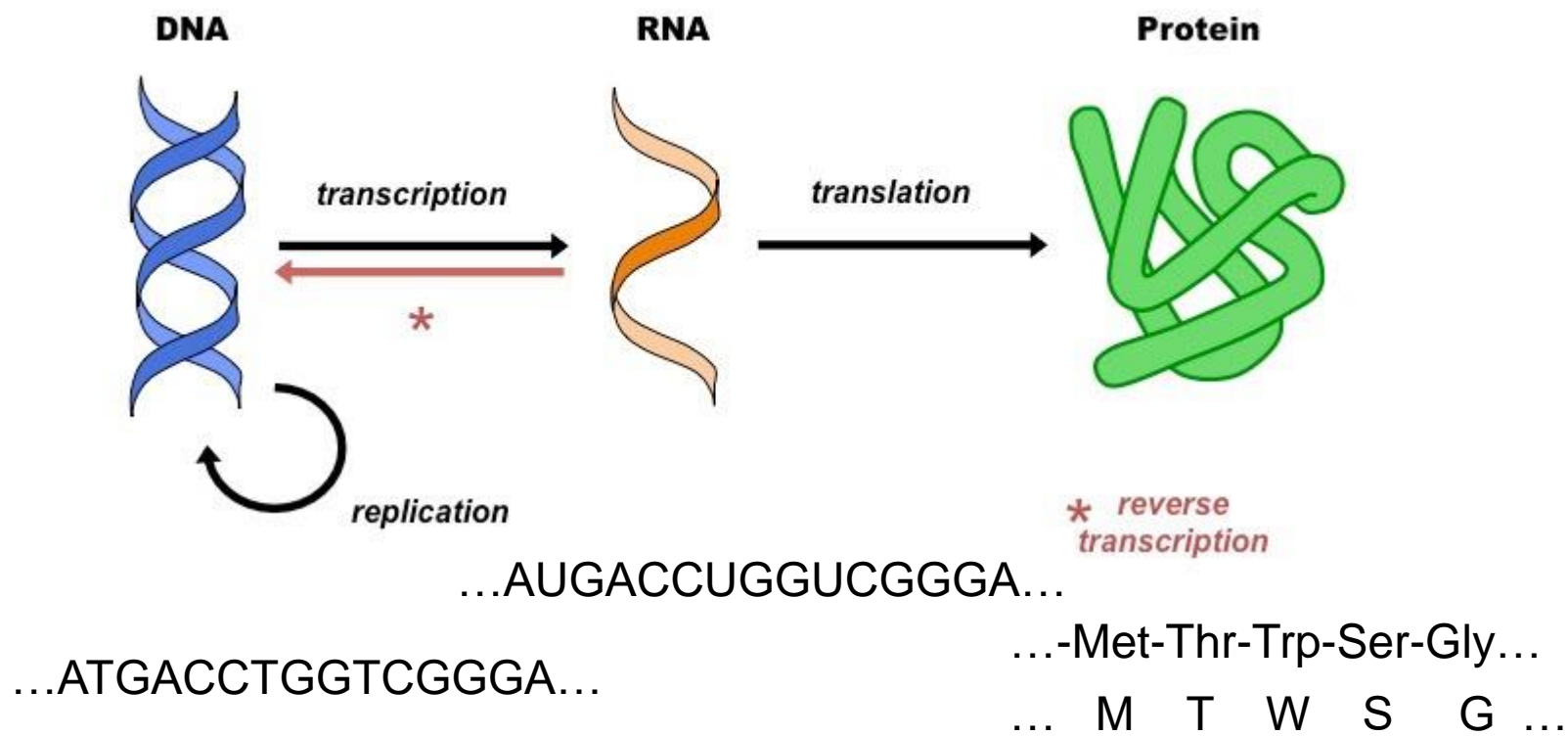
Each cell:

- 46 human chromosomes
- 2 meters of DNA
- 3 billion DNA subunits (the bases: A, T, C, G)
- Approximately 30,000 genes code for proteins that perform most life functions



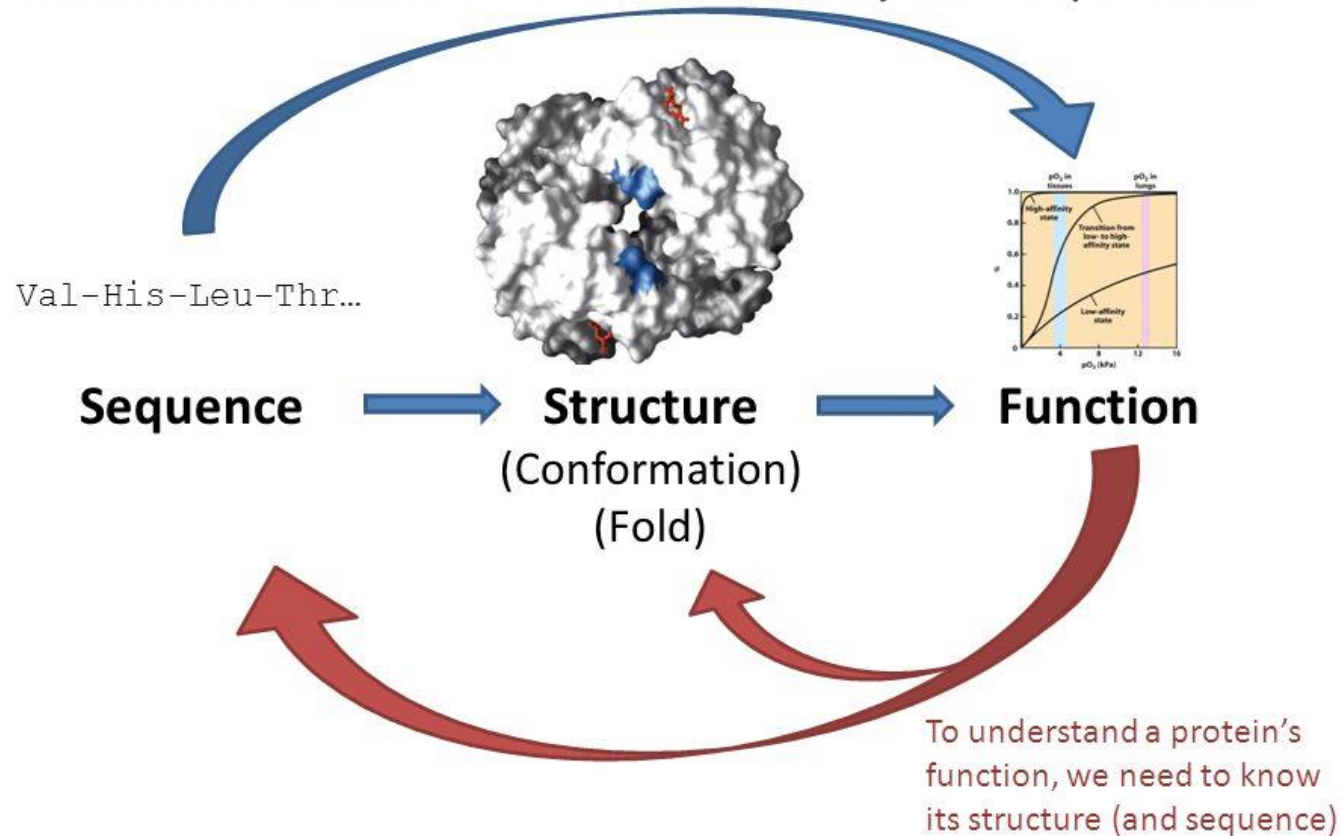
Central dogma of molecular biology

- DNA and RNA alphabet: 4-letter (base pairs)
- Protein alphabet: 20-letter (amino acid residues)

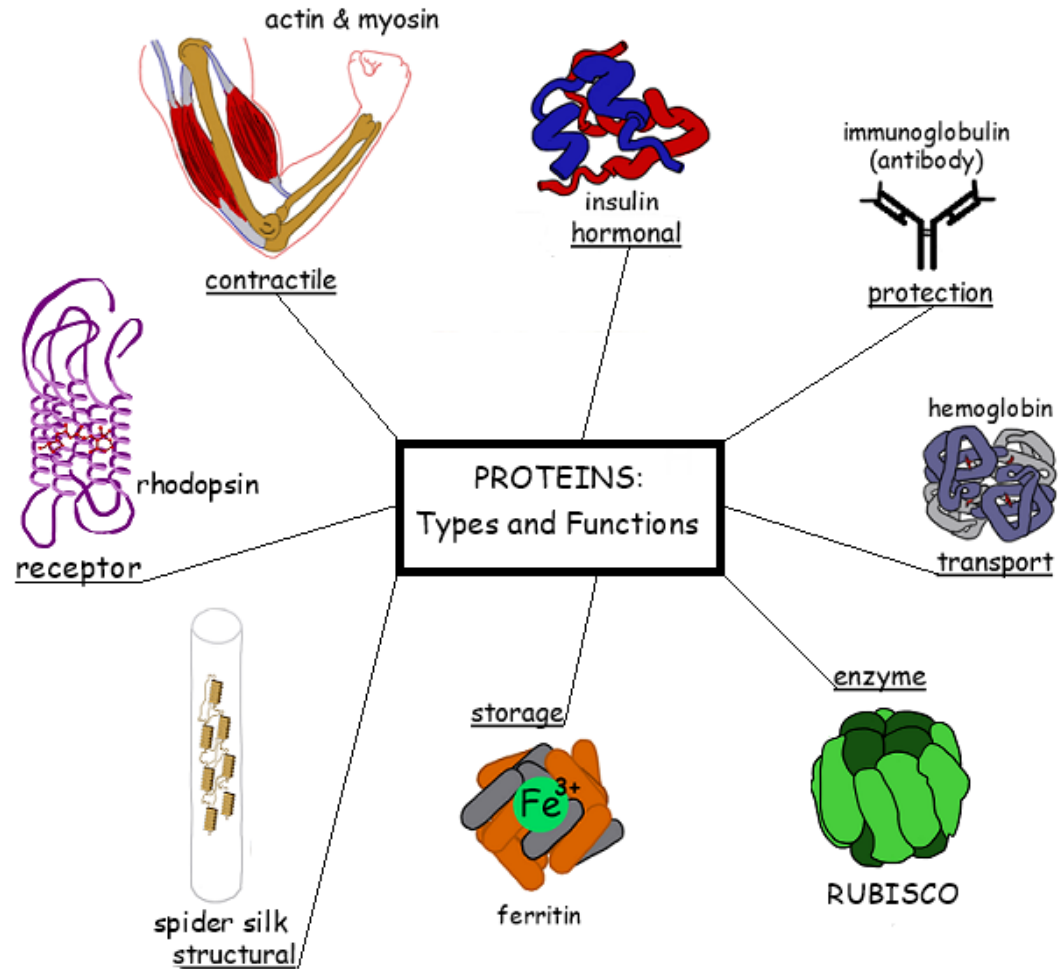


Proteins: sequence, structure, function

A protein's function derives from its structure, and its structure is determined by its sequence.



Proteins perform all functions

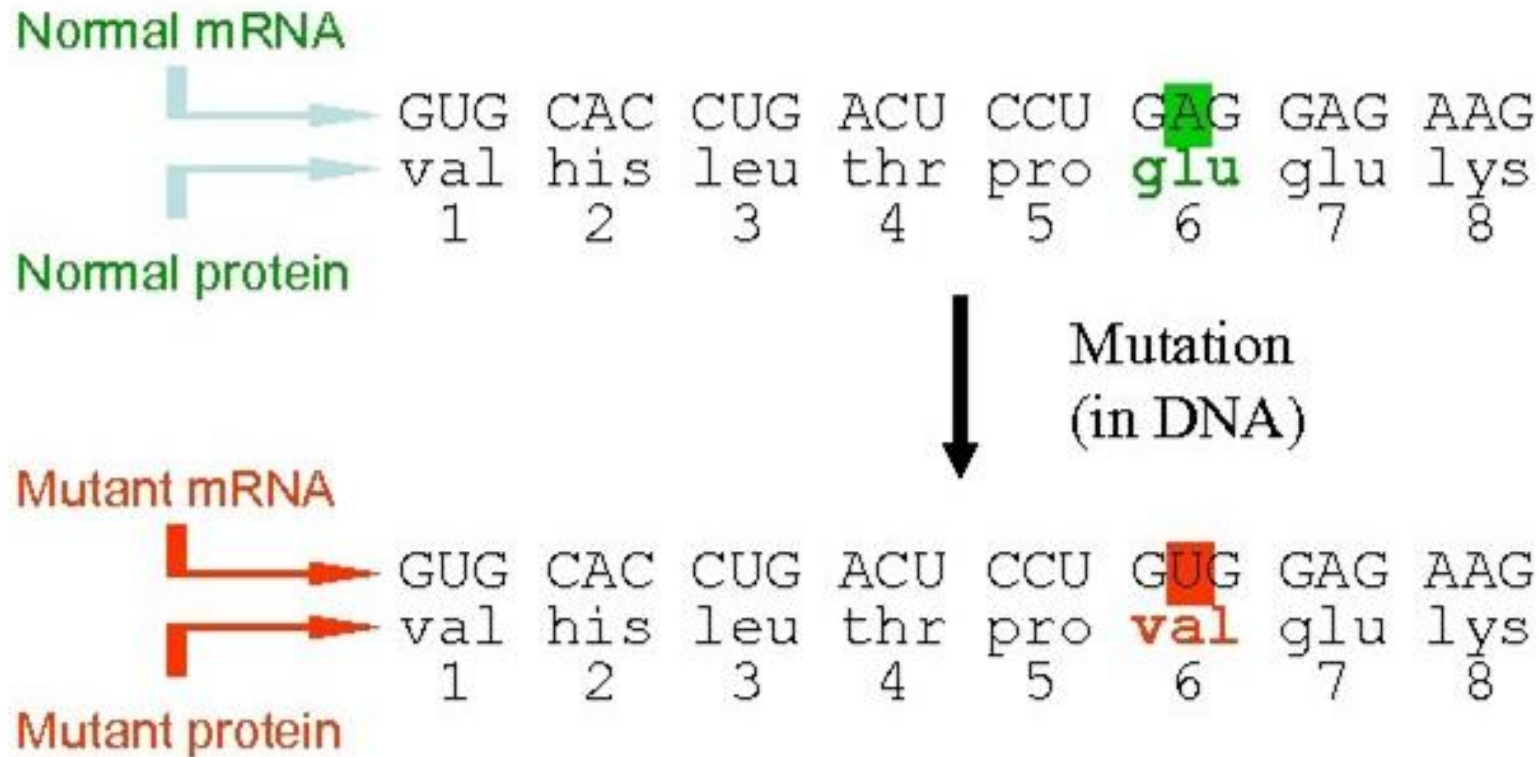


Genetic code

		Second letter				
		U	C	A	G	
First letter	U	UUU } Phe UUC } UUA } Leu UUG }	UCU } UCC } Ser UCA } UCG }	UAU } Tyr UAC } UAA Stop UAG Stop	UGU } Cys UGC } UGA Stop UGG Trp	U C A G
	C	CUU } CUC } Leu CUA } CUG }	CCU } CCC } Pro CCA } CCG }	CAU } His CAC } CAA } Gln CAG }	CGU } CGC } Arg CGA } CGG }	U C A G
	A	AUU } AUC } Ile AUA } AUG Met	ACU } ACC } Thr ACA } ACG }	AAU } Asn AAC } AAA } Lys AAG }	AGU } Ser AGC } AGA } Arg AGG }	U C A G
	G	GUU } GUC } Val GUA } GUG }	GCU } GCC } Ala GCA } GCG }	GAU } Asp GAC } GAA } Glu GAG }	GGU } GGC } Gly GGA } GGG }	U C A G

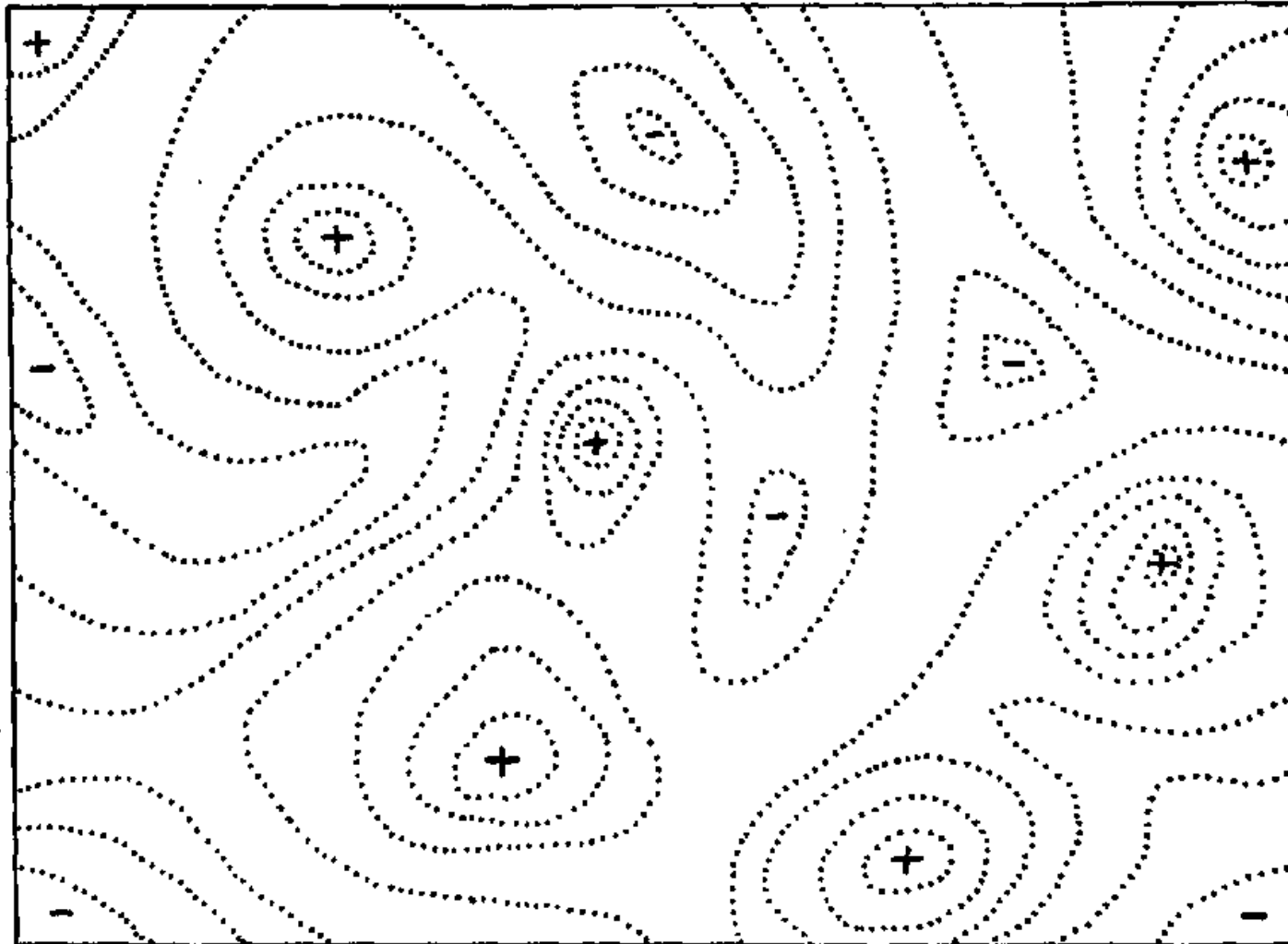
Third letter

Mutations



Glutamate (**glu**), a negatively charged amino acid, is replaced by valine (**val**), which has no charge.

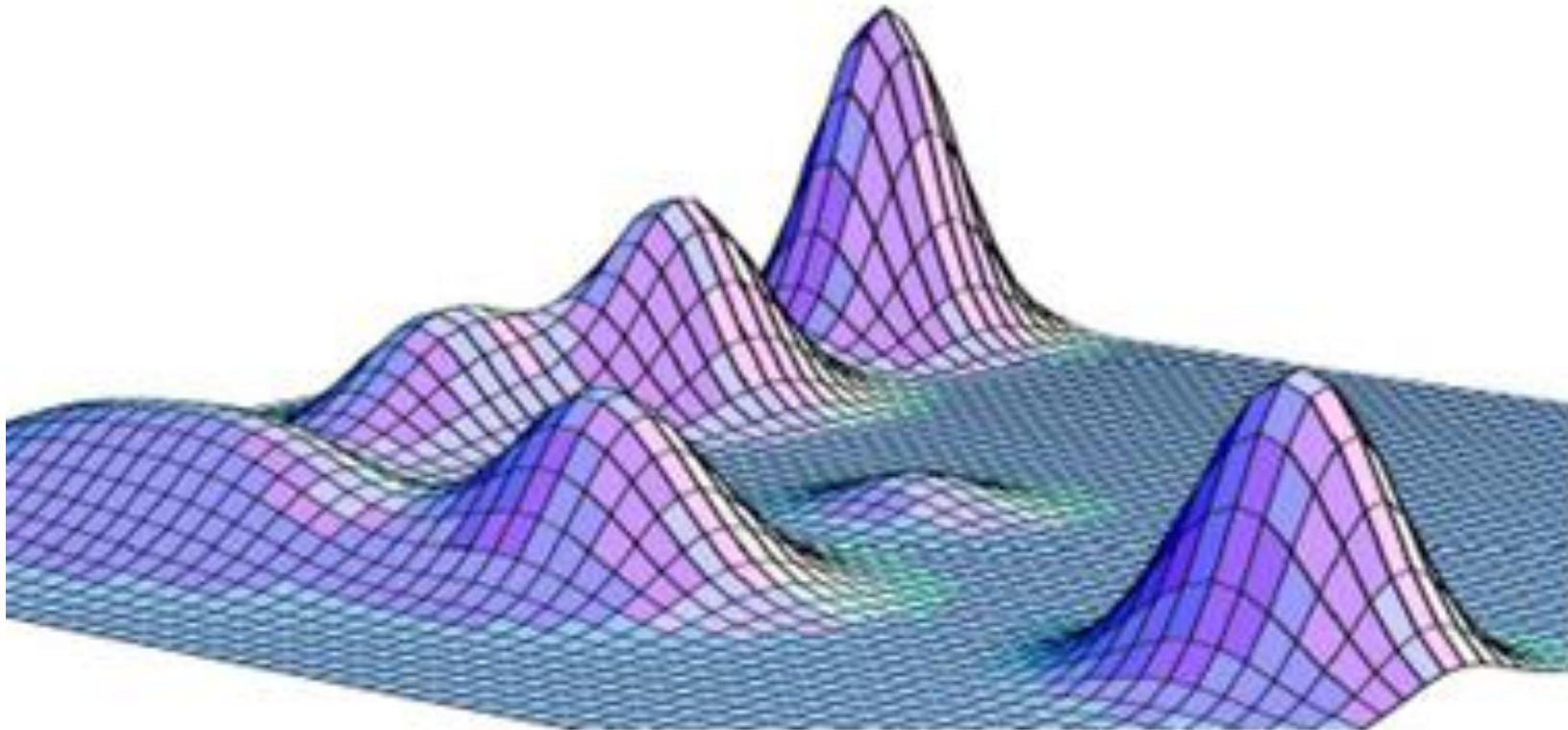
Fitness landscape concept



Fitness landscape: side view

Size of genome: 3,200,000,000 nt

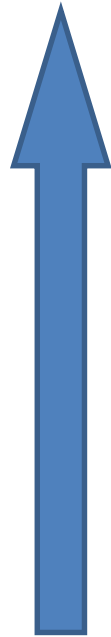
Size of genotype space: $4^{3,200,000,000}$ – impossibly large



Holy Grail of evolutionary biology

- Genotype-to-phenotype connection

Phenotype and fitness

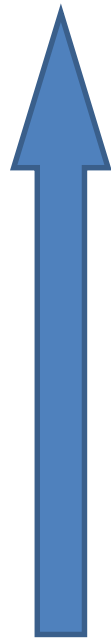


Genotype

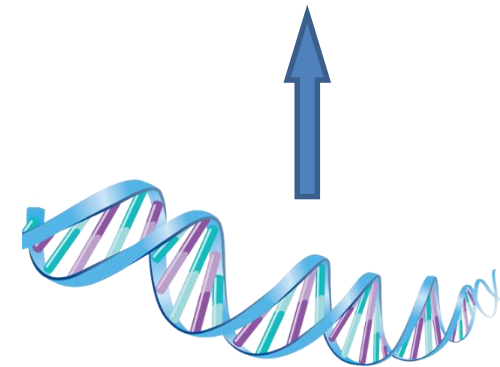
Holy Grail of evolutionary biology

- Genotype-to-phenotype connection

Phenotype and fitness








Genotype



...ACCGTAGTTGTGAAACTATAC...

Genome size

- However, the number of variants is huge:

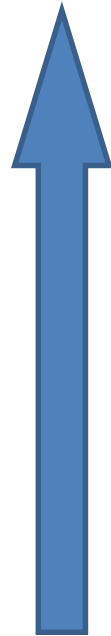
Species	<i>T2 phage</i>	<i>Escherichia coli</i>	<i>Drosophila melanogaster</i>	<i>Homo sapiens</i>	<i>Paris japonica</i>
Genome Size	170,000 bp	4.6 million bp	130 million bp	3.2 billion bp	150 billion bp
Common Name	 Virus	 Bacteria	 Fruit fly	 Human	 Canopy Plant

- For human-size genome it is $4^{3,200,000,000}$ variants
- Experimentally impossible, prediction – we don't understand much

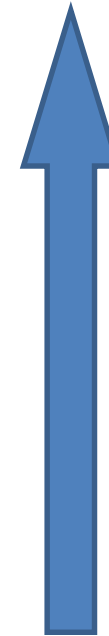
Approach to prediction

Phenotype and fitness

Change of phenotype and fitness



Genotype



Change of genotype

Predictability

MVYKERWHMPRL - crocodile
MVYKEPWHMPRL - tamandua

Null hypothesis:

If an amino acid state is good enough for the crocodile,
It ought to be good enough for the southern tamandua.

MVYPEPWCMPRM
VVYPEPWCMPRL
MVYPEPWHMPRL
MTFPEDYCMPL
TTFPHDWCMPRL
TTFPEDWCMPRL
MVYPEPWCMPRL
MVYPEPWCMPGL
MVYPEPYCMPL
MVYKERWHMPRL
MVYKEPWHMPRL
MVFPEWCIPRL
MTFPEDWCIPRL
MTFPEDWCMPRL
MTFPYDWCMPRL
MTFPHDWQMPRL
MTYPHDLMPRL
MTFPHDFCMPRL
MTFPHDLMPRL
MMYPHDFCMPRL

Predictability

It would be easier to predict if the effect of a substitution is universal

Then, for human we would have to measure the effect of just all

$3 * 3,200,000,000$ single mutations (universal effect)

which looks reasonable instead of

$4^{3,200,000,000}$ variants (full dependence)

Epistasis

However, it is not always true:

Epistasis – dependence of mutation effect
on genetic context

Epistasis as a word game

WORD^{D4E} – WORE^{W1G} – GORE^{R3N} – GONE^{O2E} – GENE

R3N

~~WONE~~

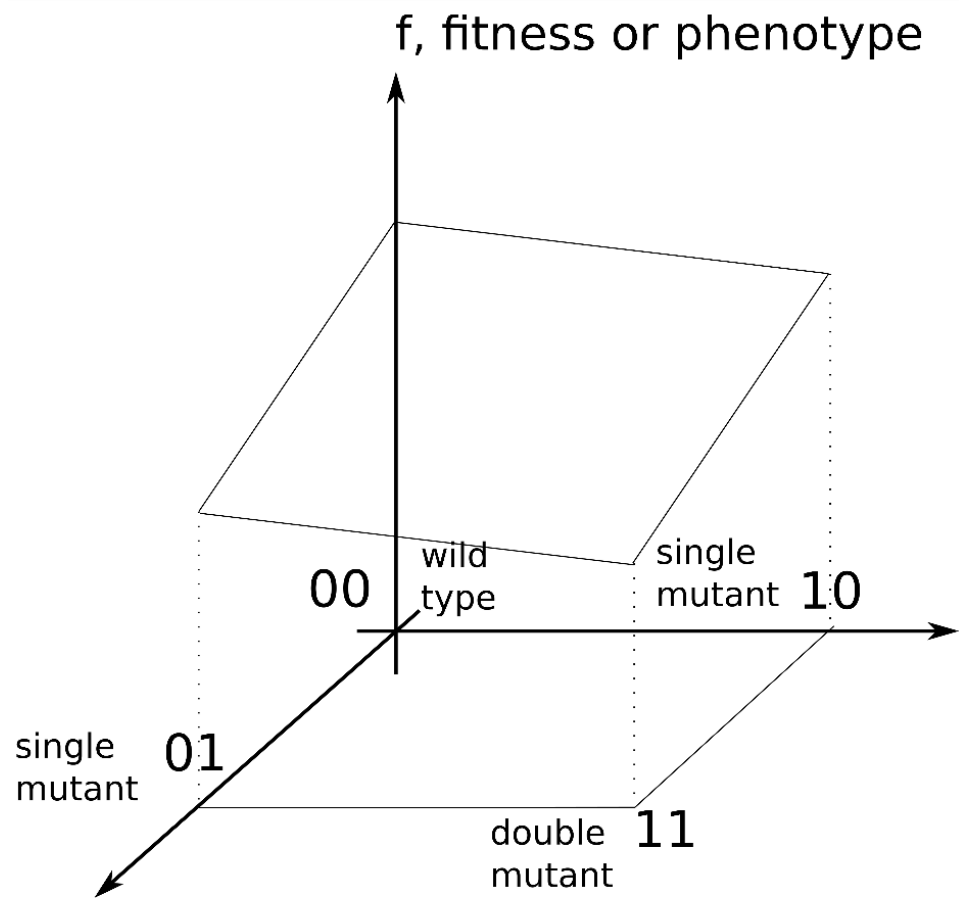
Life examples

- Non-epistatic logic (predictability) :
 - “If English was good enough for Jesus, then it will be good enough for Texas children” (Texas governor, ~1930)

Life examples

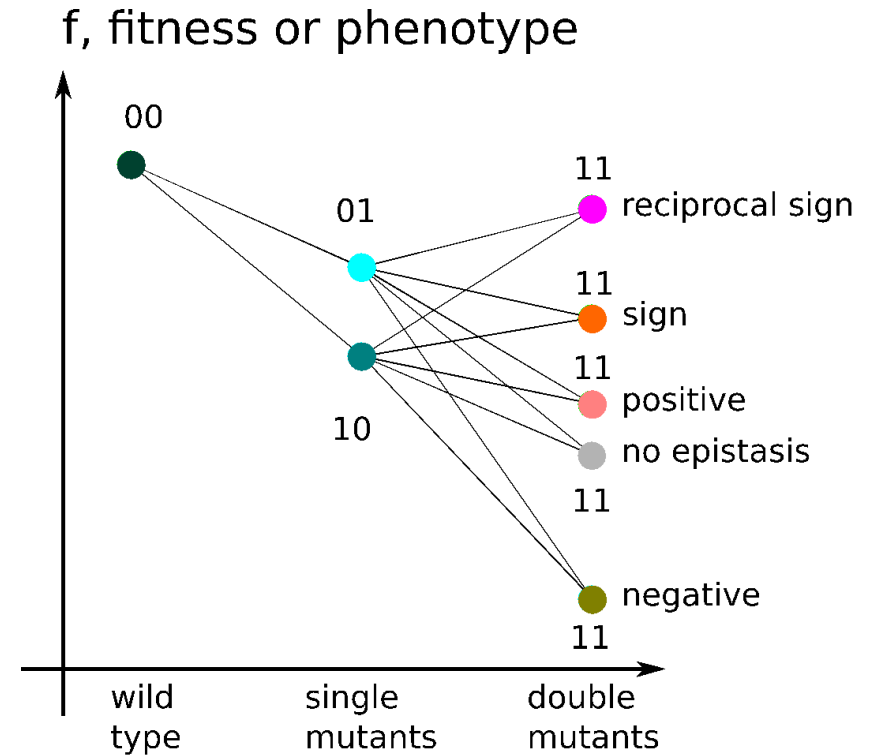
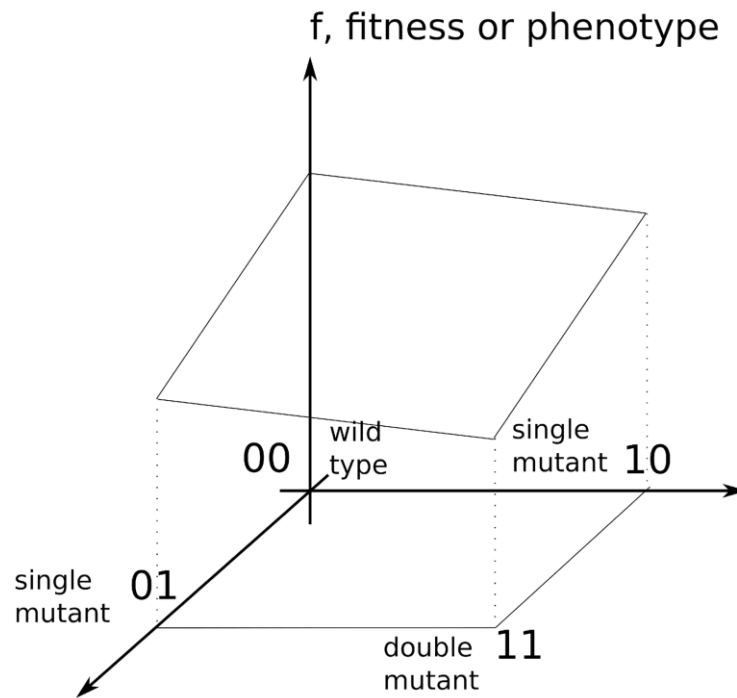
- Non-epistatic logic (predictability) :
 - “If English was good enough for Jesus, then it will be good enough for Texas children” (Texas governor, ~1930)
- Epistatic logic (no predictability):
 - What is good for Russian, is mortal for German
/ Что русскому хорошо, то немцу смерть /
 - Spoon is good at lunchtime
/ Хороша ложка к обеду /

Visualization of epistasis



Types of epistasis

- Epistasis – non-additive effect of substitutions
- No epistasis – full predictability



Formal definition of epistasis

effect of single substitutions

correction for triple substitutions

$$f(g) = \underset{\text{reference level}}{const} + \sum_{i=1}^N \alpha_i \delta_i + \sum_{i=1}^N \sum_{j=1}^N \alpha_{ij} \delta_i \delta_j + \sum_{i=1}^N \sum_{j=1}^N \sum_{k=1}^N \alpha_{ijk} \delta_i \delta_j \delta_k + \dots$$

correction for double substitutions

Higher-order epistasis

The diagram illustrates the formal definition of epistasis through a mathematical equation. The equation is $f(g) = const + \sum_{i=1}^N \alpha_i \delta_i + \sum_{i=1}^N \sum_{j=1}^N \alpha_{ij} \delta_i \delta_j + \sum_{i=1}^N \sum_{j=1}^N \sum_{k=1}^N \alpha_{ijk} \delta_i \delta_j \delta_k + \dots$. Labels with arrows point to specific parts of the equation: 'reference level' points to 'const'; 'effect of single substitutions' points to the first summation term; 'correction for double substitutions' points to the second summation term; 'correction for triple substitutions' points to the third summation term, which is enclosed in a box; and 'Higher-order epistasis' points to the ellipsis '...'.

Here: $const = f(\text{wt})$

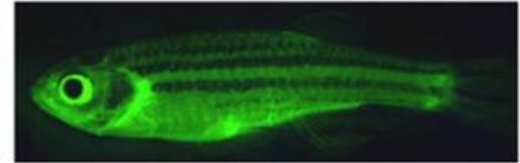
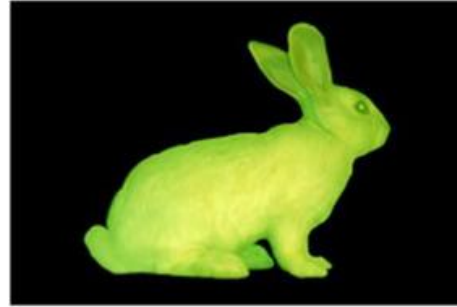
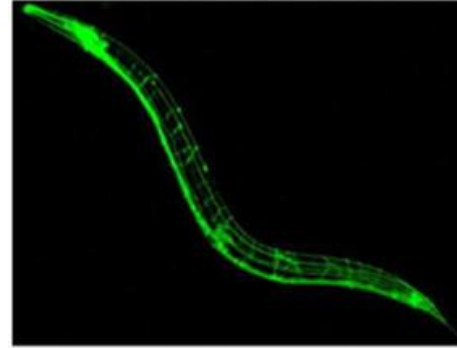
$$\delta_i = \begin{cases} 1, & \text{mutation } i \text{ is present in genotype } g \\ 0, & \text{otherwise} \end{cases}$$

Epistatic terms

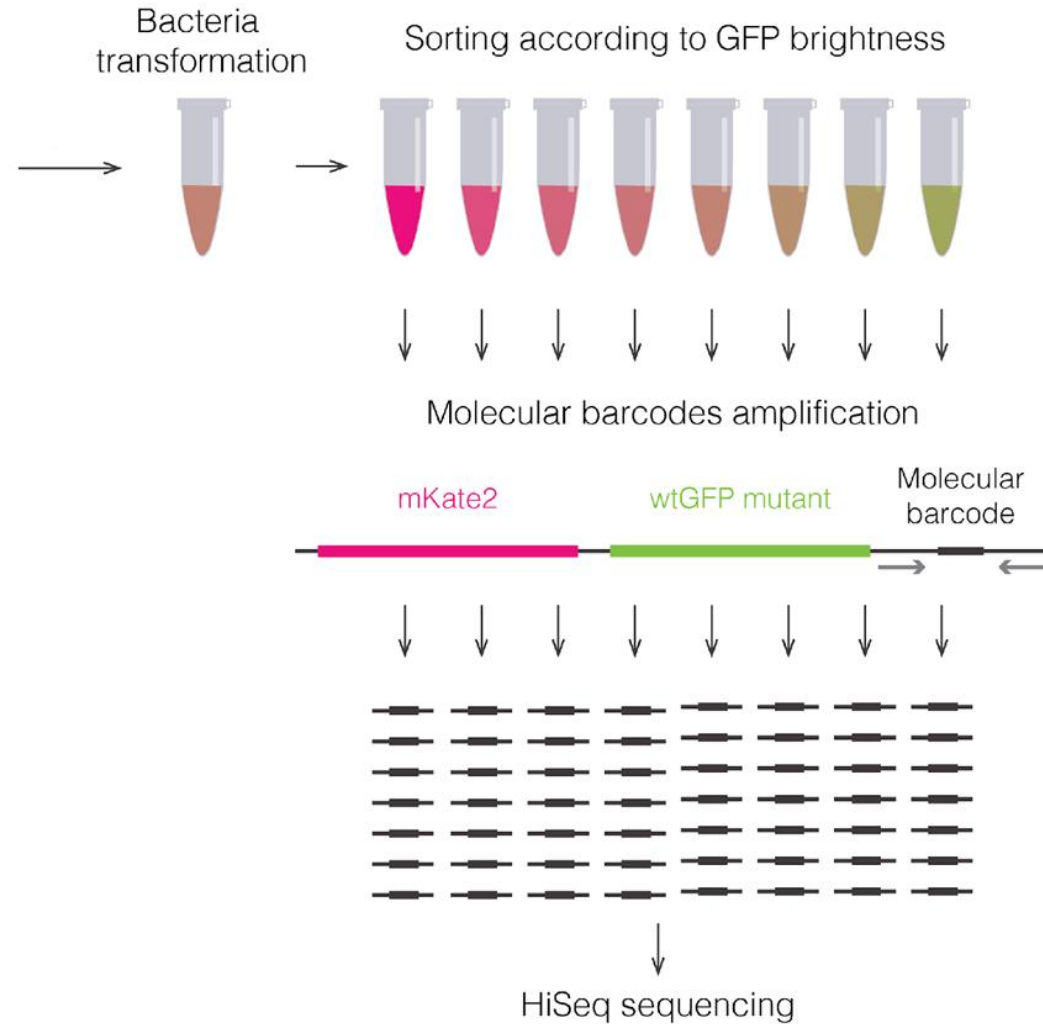
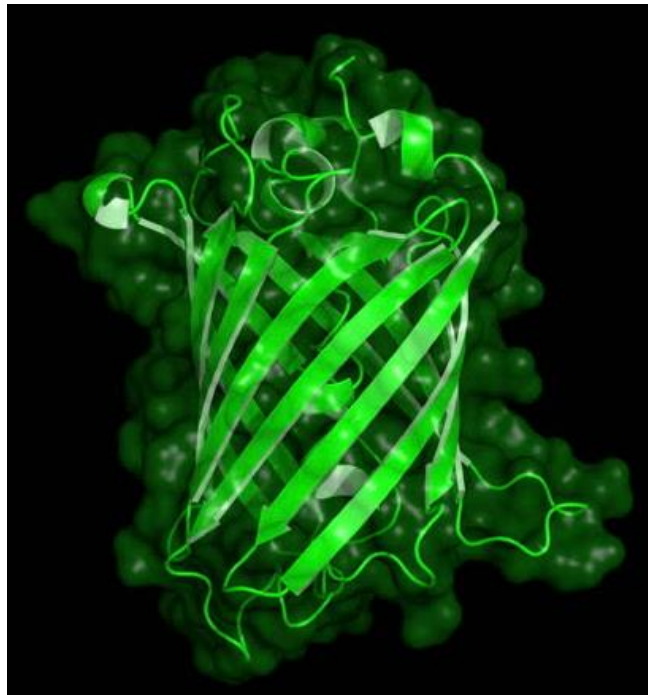
- N-order epistatic term \Rightarrow N-dimensional hypercube must be measured
- Experiments can be carefully designed to have all 2^N phenotypes
- What about random mutagenesis experiments?

Random mutagenesis experiment in green fluorescent protein (GFP)

GFP, Nobel prize 2008

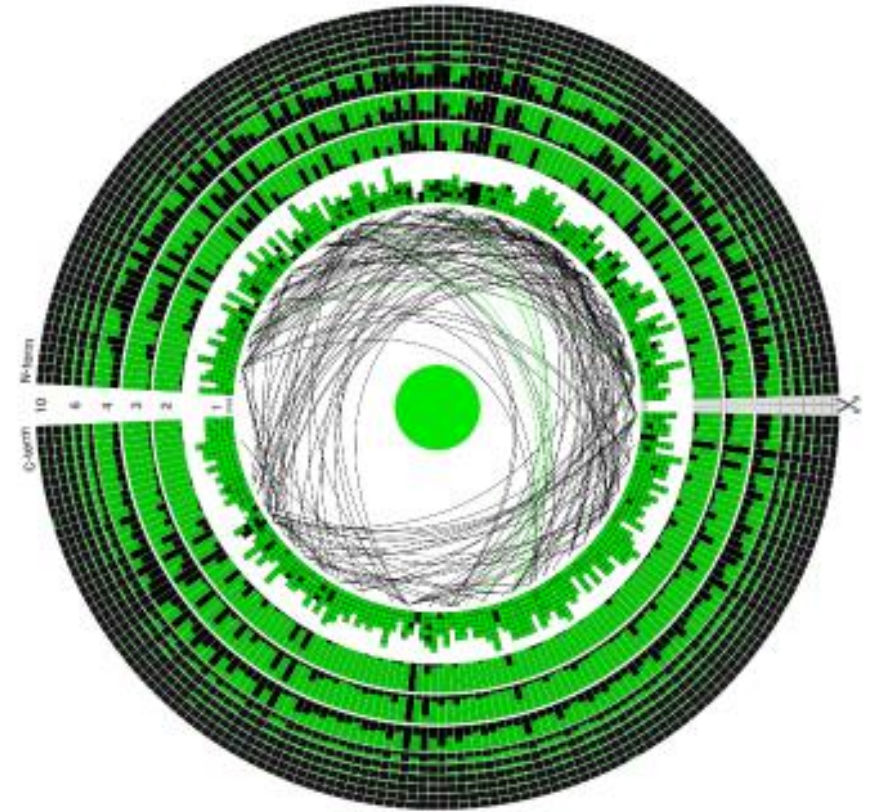


Experiment



Random mutagenesis in GFP

- ✓ 56,086 unique nucleotide sequences
- ✓ 51,715 unique amino acid sequences
- ✓ 238 amino acid residues
- ✓ 1817 types of single mutations
- ✓ 50% of the population lose fluorescence after 5 mutations



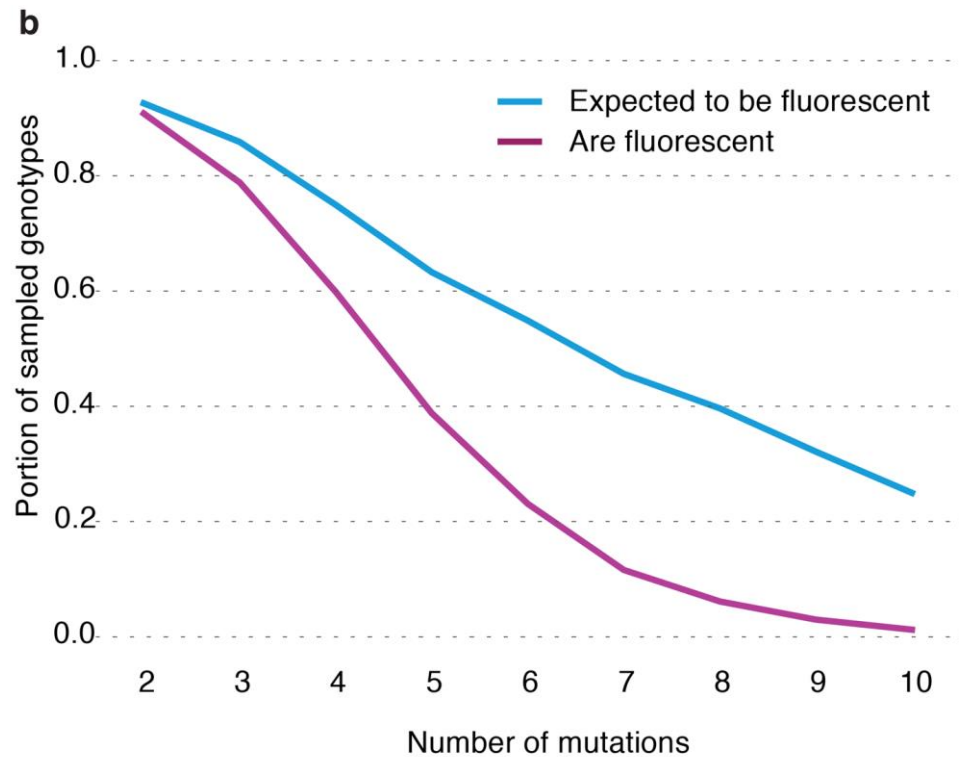
Random mutagenesis data

#	genotype	phenotype
1	A24G	0.95
2	S56T	0.1
3	A24G; C170M	0.97
4	A24G; S56T; C170M	0.07
...

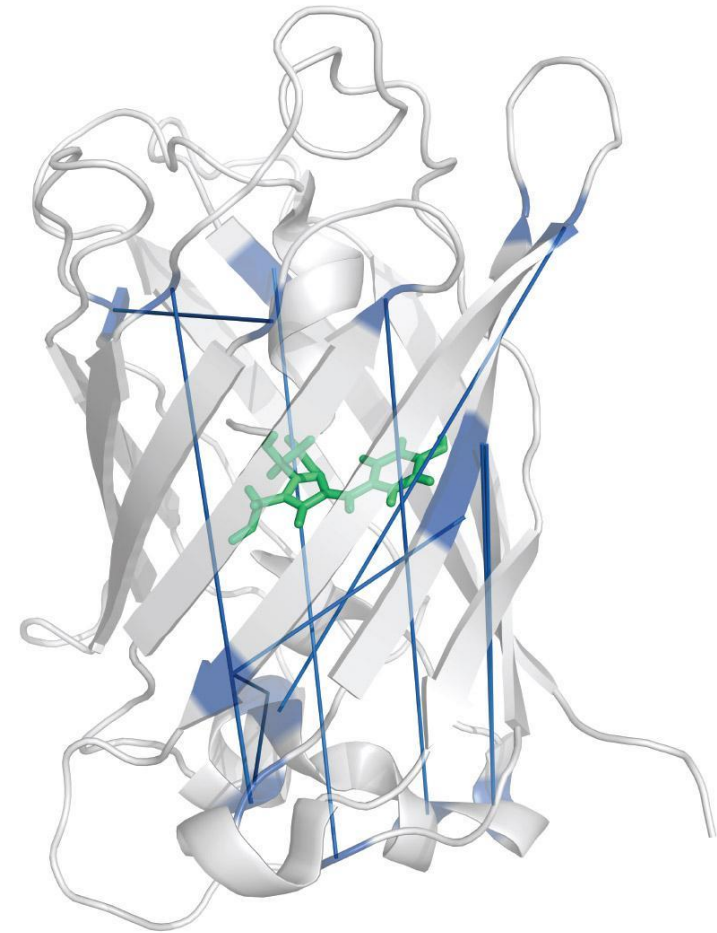
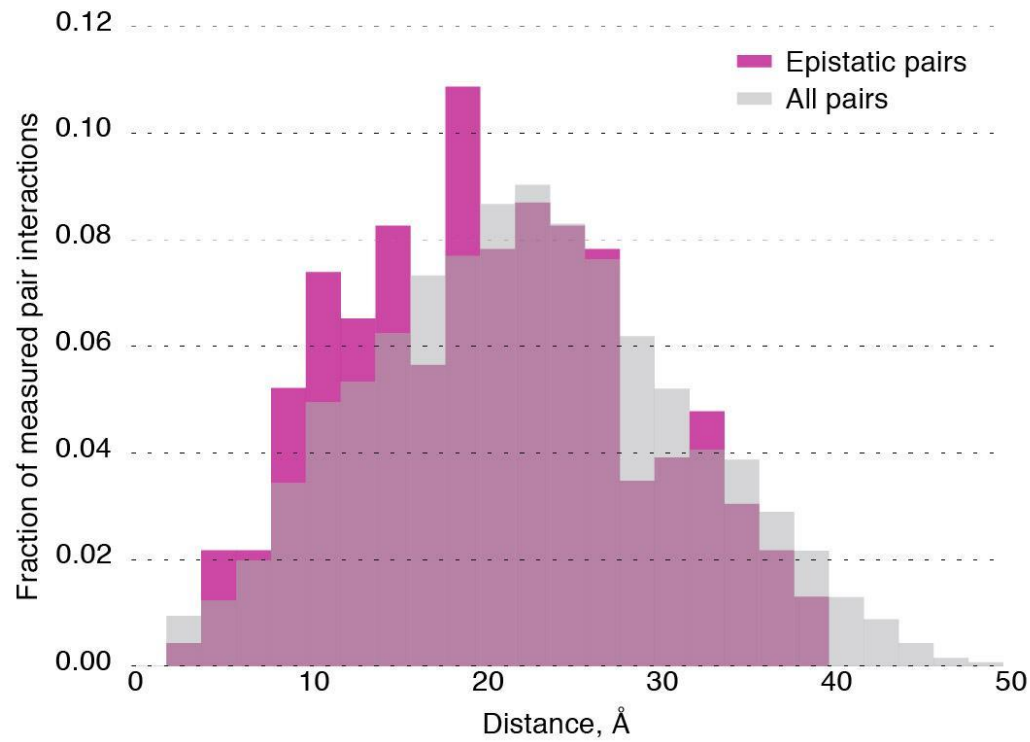
of measured genotypes:

- GFP: 51 715

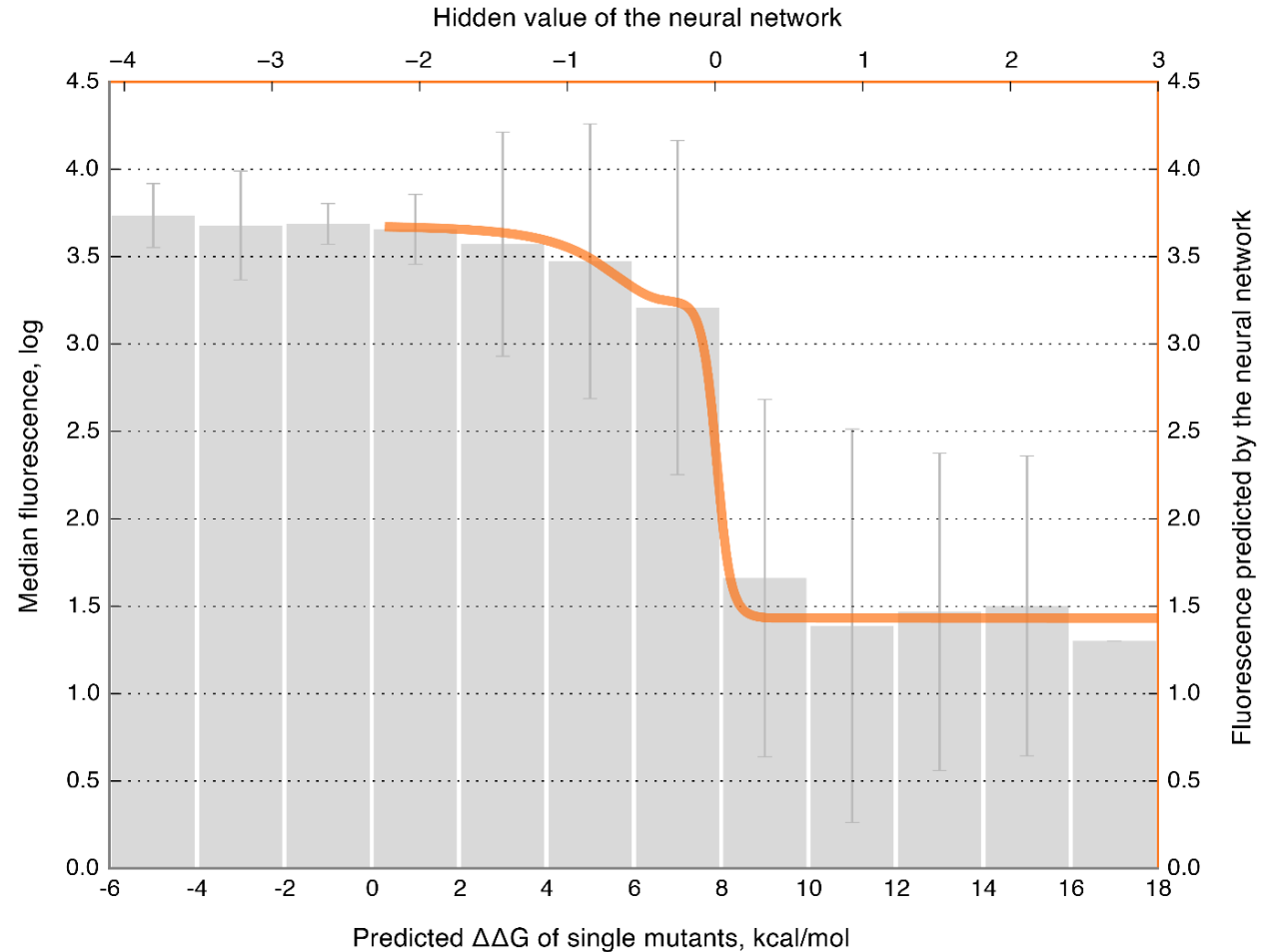
Expected vs. observed effects



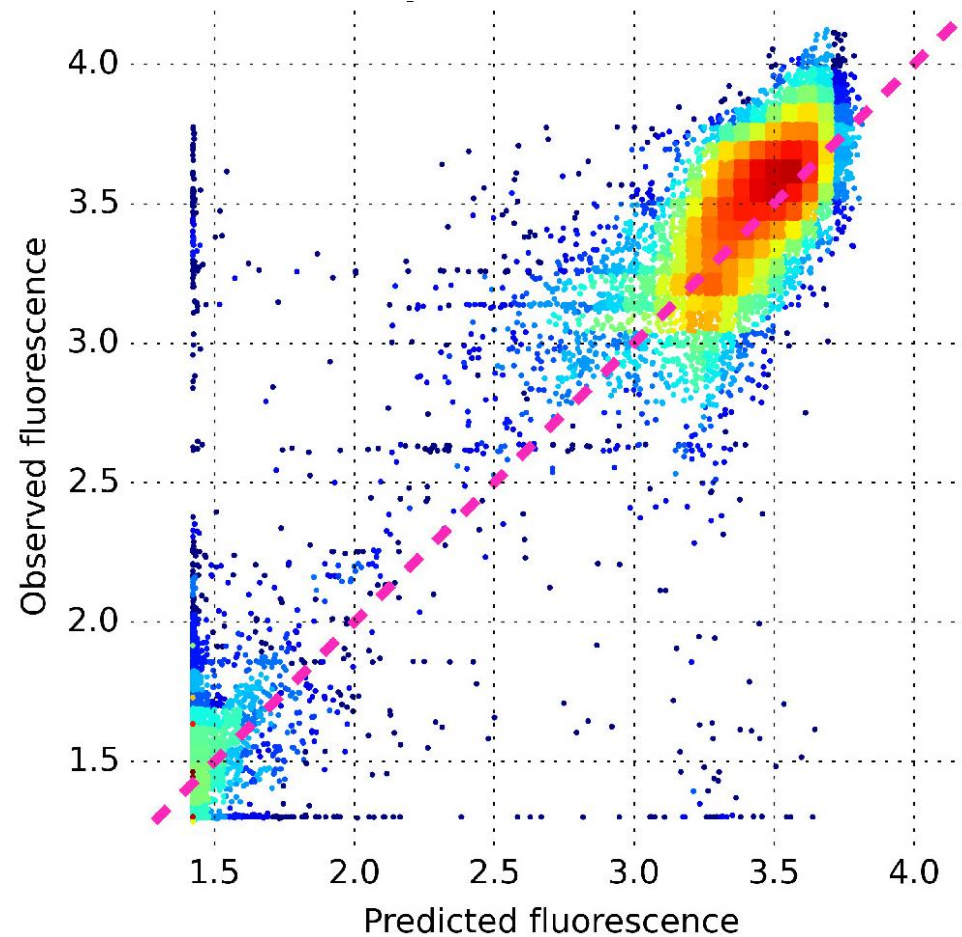
Epistatic pairs on GFP structure



Protein stability as explanation



Observed vs. predicted



Conclusion #1

- ✓ 93% of epistasis was explained by change of protein stability
- ✓ 6% of epistasis remained unexplained

Quasi-random mutagenesis experiment in yeast HIS3 protein

HIS3 as the next model

- ✓ 220 amino acids long
- ✓ Is essential for Histidine synthesis, conditionally essential for yeast growth
- ✓ Present in a single copy
- ✓ Relatively conservative protein sequence

```

-----MTEQKALVKRITNETKIQIAISLKGGLAIEHSIF-----PEKEAEAVAEQATQSQVINVHTGIGFLDHMIH
-----MSETQQAFVKRYTPLRSPNSLALNGGPFIEIGQSIL-----GGAKTTVAHQASSQVINVQTGVGFLDHMIH
-----MSEQKALVKRITNETKIQIAIALKGGPLALEHSIF-----PAREADAVAEQATQSQVINVQTGIGFLDHMVH
-----MAFVKRVTEQETNIQLALDLDGGSVSVRESIL-----GKEYASGDGQTIHVHTGVGFLDHMLT
MAQEQQEQRALINRITNETKIQIAISLKGGLPLTQSSIF-----PTKESNVATQATSSQVIDIHTGVGFLDHMIH
---MTYPERKAFVSRITNETKIQIAISLNGGPISSIENSIL-----QREESDAAKQVTGSQIIDIQTVGVGFLDHMIH
-----MAKTATIKRDTNETKIQIAISLEGGHIALEESIFKNSANETKDDSHATQATSTQVIQVQTVGIGFLDHMLH
-----MSSERKAFVKRDTNETKIQIALSLDGGAVSIPTSIL---PKNDKVEDHAIQKTGGQVINVQTGIGFLDHMLH
-----MRRAFVERNTNETKISVAIALDKAPLPEESNFI-----DELITSKHANQKGEQVIQVDTGIGFLDHMYH

```

```

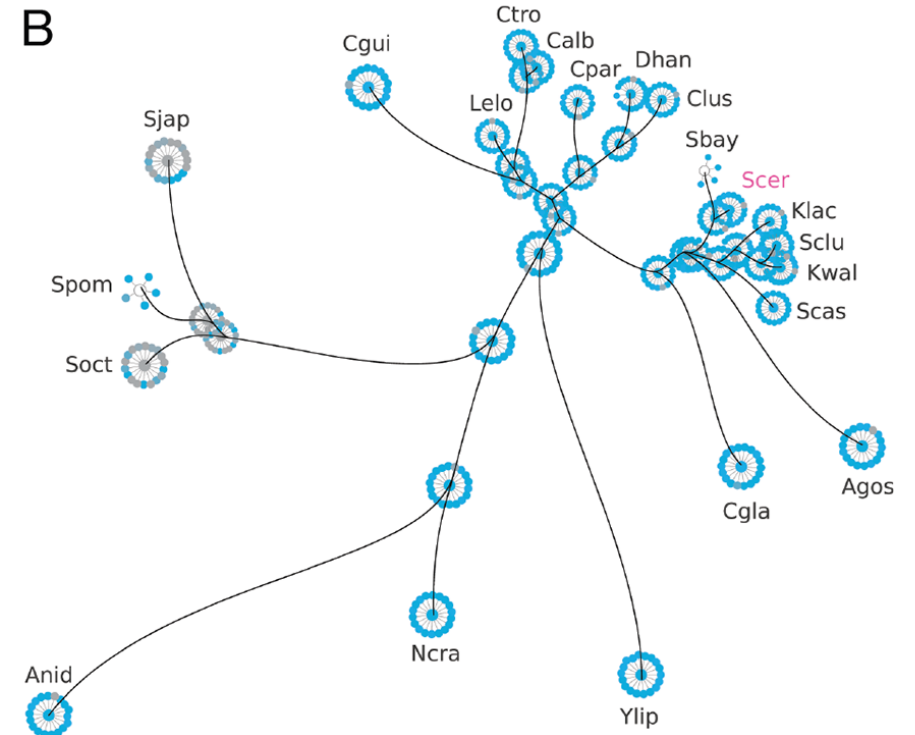
ALAKHSGWSLIVEICIGDLHIDDHHTTEDCGIALGQAFKEALGAVRGVVKRFGSGFAPLDEALSRAVVDLSNRPFYAVV
ALAKHSGWSLIVEICVGLHIDDHHTTEDCGIALGQALREAIQVVRGVKRFGTGFAPLDEALSRAVVDLSNRPFYAVV
ALAKHAGWSLIVEICIGDLHIDDHHTTEDCGIALGQAFKEALGAVRGVVKRFGSGFAPLDEALSRAVVDLSNRPFYAVV
ALAKHGGWSLILECIGDLHIDDHHTVEDCGIALGQAFKEALGAVRGVVKRFGSGFAPLDEALSRAVVDLSNRPFYAVV
ALAKHAGWSLIVEICIGDLHIDDHHTTEDCGIALGQAFKEAMGVVRGVKRFGTGFAPLDEALSRAVVDLSNRPFYAFI
ALAKHSGWSLIVEICIGDLHIDDHHTTEDCGIALGQAFKEALGHVVRGVKRFSGYAPLDEALSRAVVDLSNRPFYAVI
ALAKHSGWSLIECIGDIHIDDHHTAEDVGTITLGLAFHKALGQVKGVRFGCGFAPLDEALSRAVVDLSNRPFYAVI
ALAKHSGWSLVVEICIGDLHIDDHHTSEDVGIALGMFAFKDALGQIKGVKRFHGFAPLDEALSRAVVDLSNRPFYAVV
ALAKHAGWSLRLYSRGDLIDDHHTAEDTALGIAFKQAMGNFAGVVKRFHAYCPLDEALSRSVVDLSGRPFYAVI

```

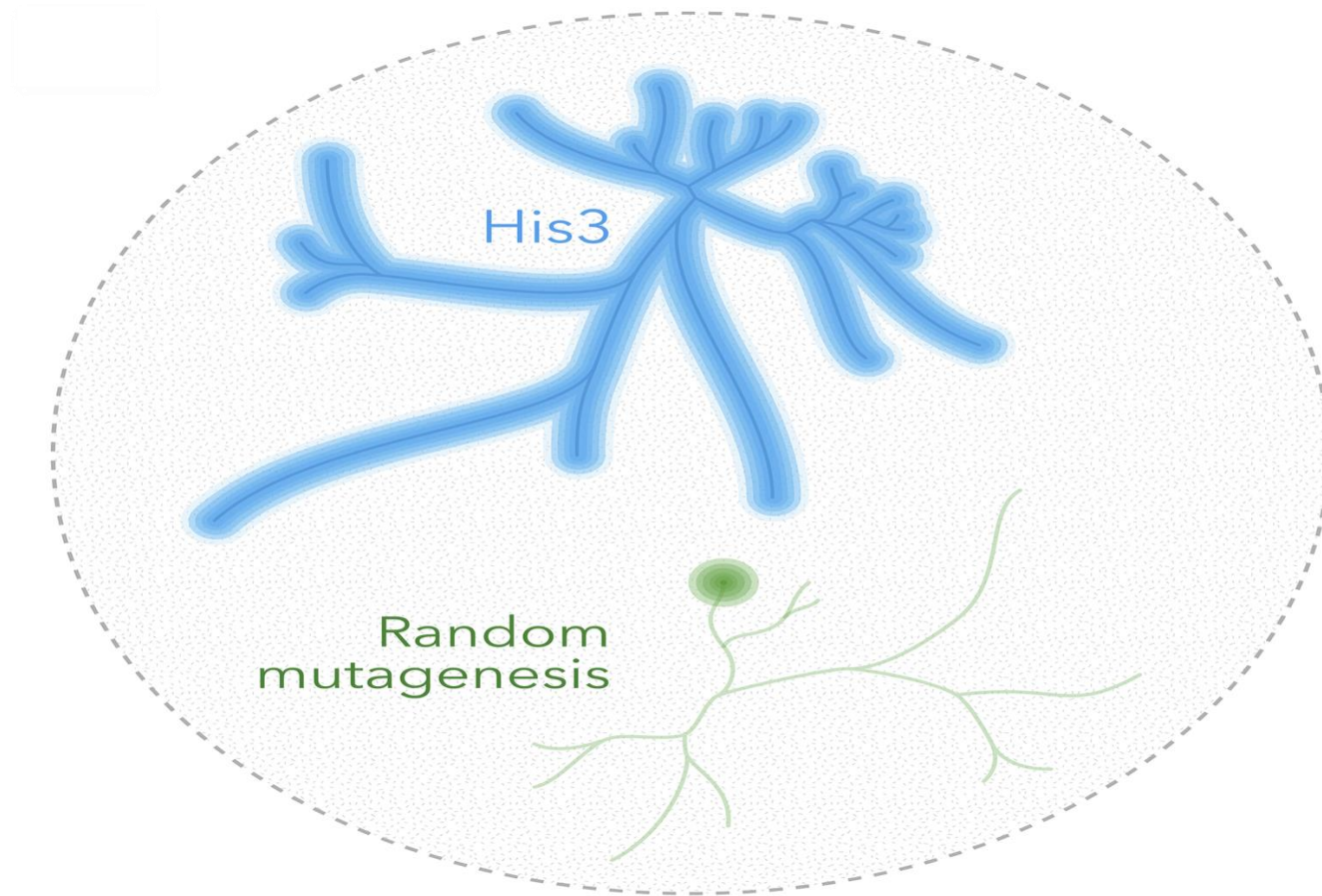
```

ELGLQREKVGDLSCEMI PHFLESFAEASRITLHVDCLRGKNDHHRSESAFKALAVAIREATSPNGTNDVPSTKGVLM
DLGLRREKIGDLSTEMI PHFLQSFASARVTLHVDCLRGTNDHHRSESAFKAVAVALGDALTRTGTDDVPSTKGVLM
ELGLQREKVGDLSCEMI PHFLESFAEASRITLHVDCLRGKNDHHRSESAFKALAVAIREATSPNGTNDVPSTKGVLM
ELGLKRERIGQLSTEMI PHFLESFATEARITMHVDCLRGTNDHHRSESAFKALAIAREARTPTGRDDVPSTKGVLA
ELGLKREKIGDLSCEMI PHFLESFAEAAARITIHVDCLRGKNDHHRSESAFKALAVAIREATSPNGTNDVPSTKGVLM
ELGLKREKIGDLSCEMI PHFLESFAEAAARITLHVDCLRGFNDHHRSESAFKALAIAREARTPTGRDDVPSTKGVLM
ELGLKREKIGDLSCEMI PHVMSFAQGAATIHVDCIRGFNDHHRSESAFKALAVAIKEATSSNGTDDVPSTKGVLF
ELGLKREKIGDLSTEMI PHVLESFAQLAATIMHVDCLRGFNDHHRSESAFKALAIAREARTPTGRDDVPSTKGVLS
DLGLKREKVGELSCEMI PHLLYSFVAAGITLHVTCLYGNSNDHHRSESAFKSLAVAMRAATSLTGSSEVPSTKGVLM

```



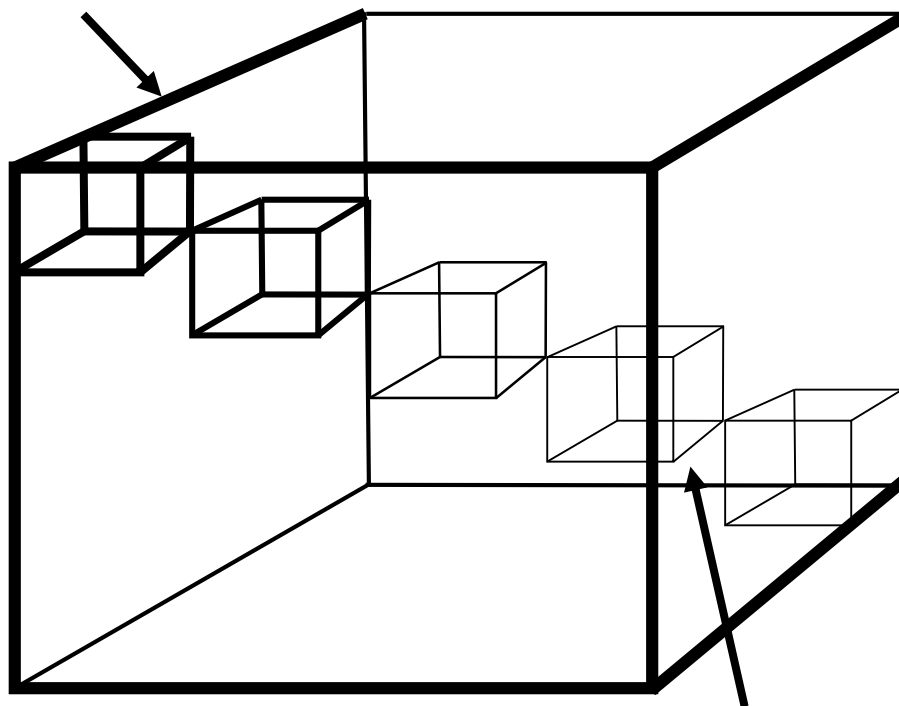
Quasi-random vs. random



Segments of HIS3

The entire sequence space of His3 has 220 dimensions and a volume of 20^{220}

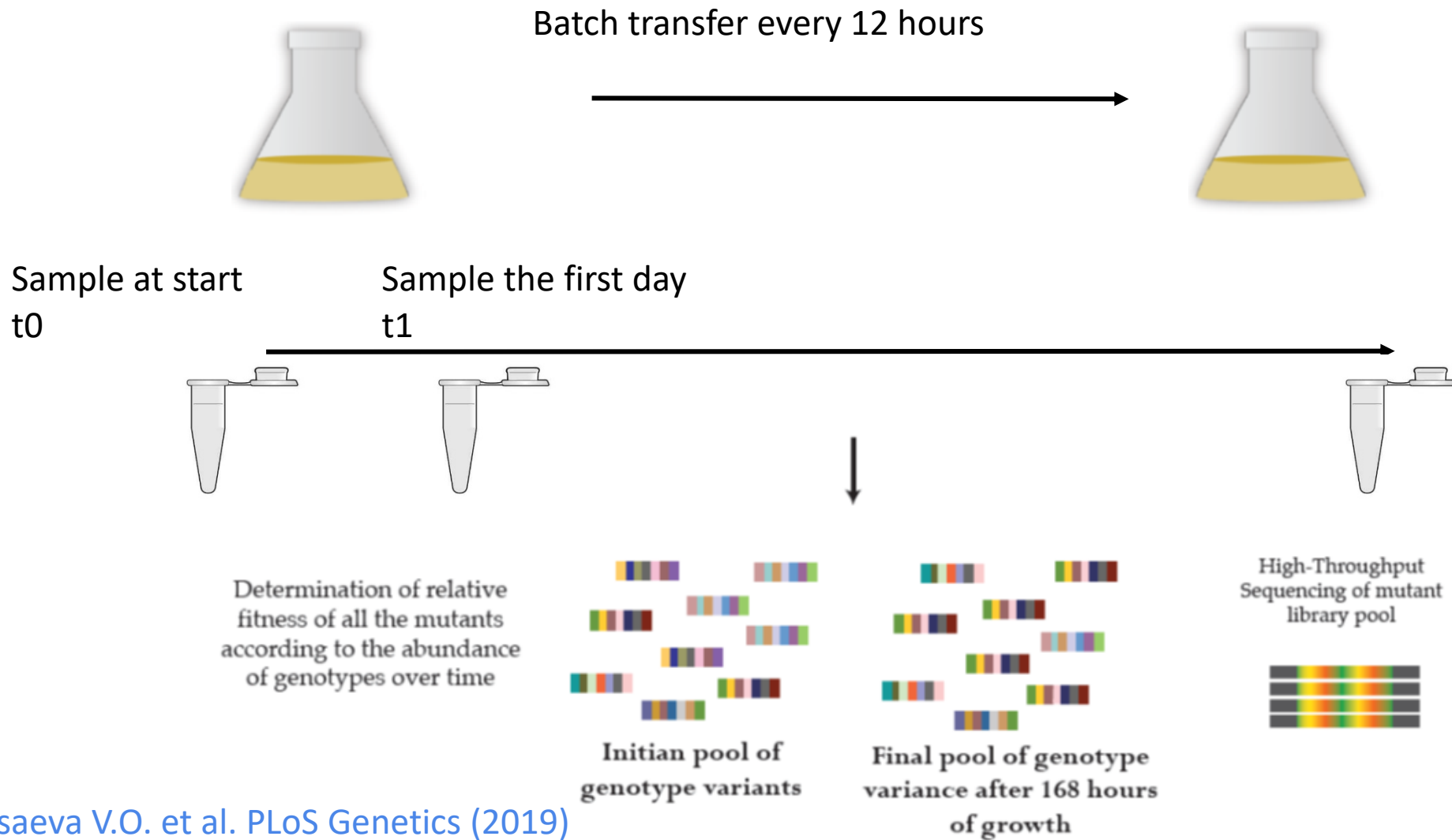
Fitness was measured for 721,791 genotypes



A subsection of His3 space is more manageable.
We study 12 segments, each 15-22 amino acids long.

Pokusaeva V.O. et al. PLoS Genetics (2019)

The HIS3 experiment



Data structure is the same

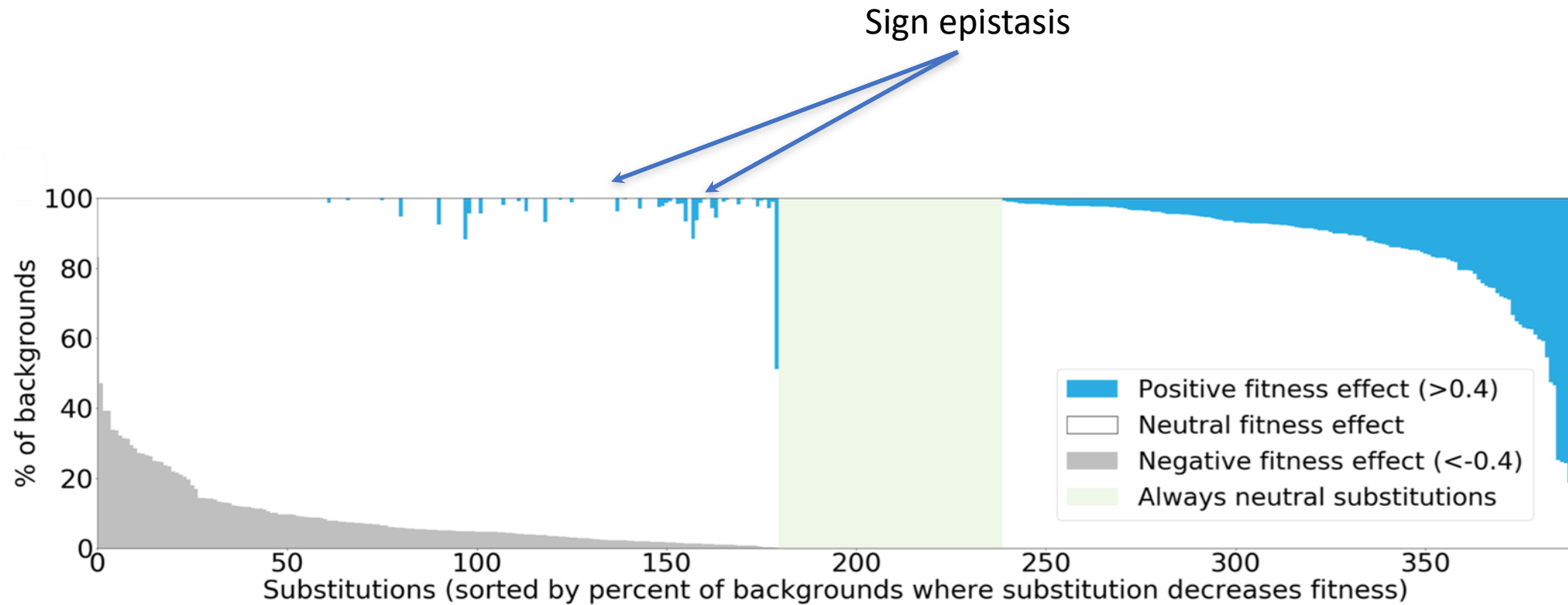
#	genotype	phenotype
1	A4G	0.95
2	C6T	0.68
3	A4G:C10M	0.35
4	A24G:S56T:C170M	0.02
...

of measured genotypes:

- His3: 721 791:

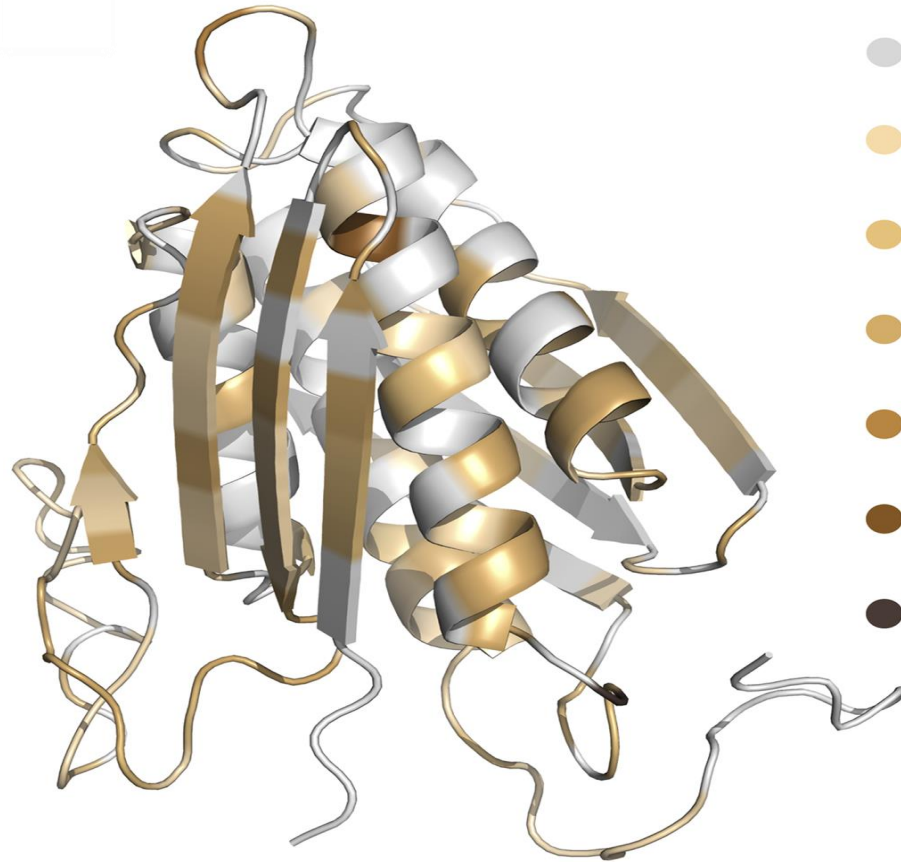
- 12 segments, from 16 000 to 82 000 genotypes

Sign epistasis in HIS3

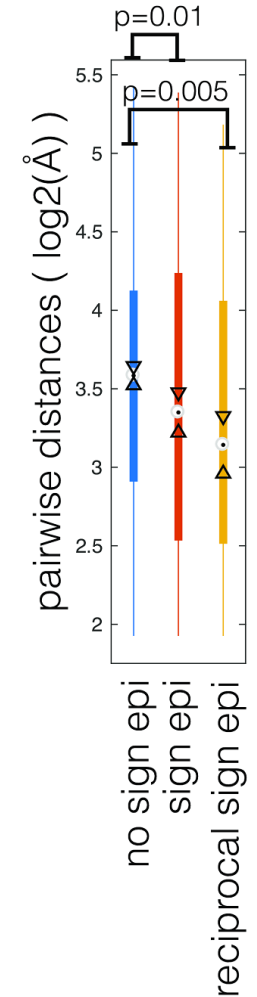


Only 15% of substitutions are universally neutral

Epistatic pairs on HIS3 structure



- 1 amino acid states assayed
- 2 amino acid states assayed
- 3 amino acid states assayed
- 4 amino acid states assayed
- 5 amino acid states assayed
- 6 amino acid states assayed
- 9 amino acid states assayed

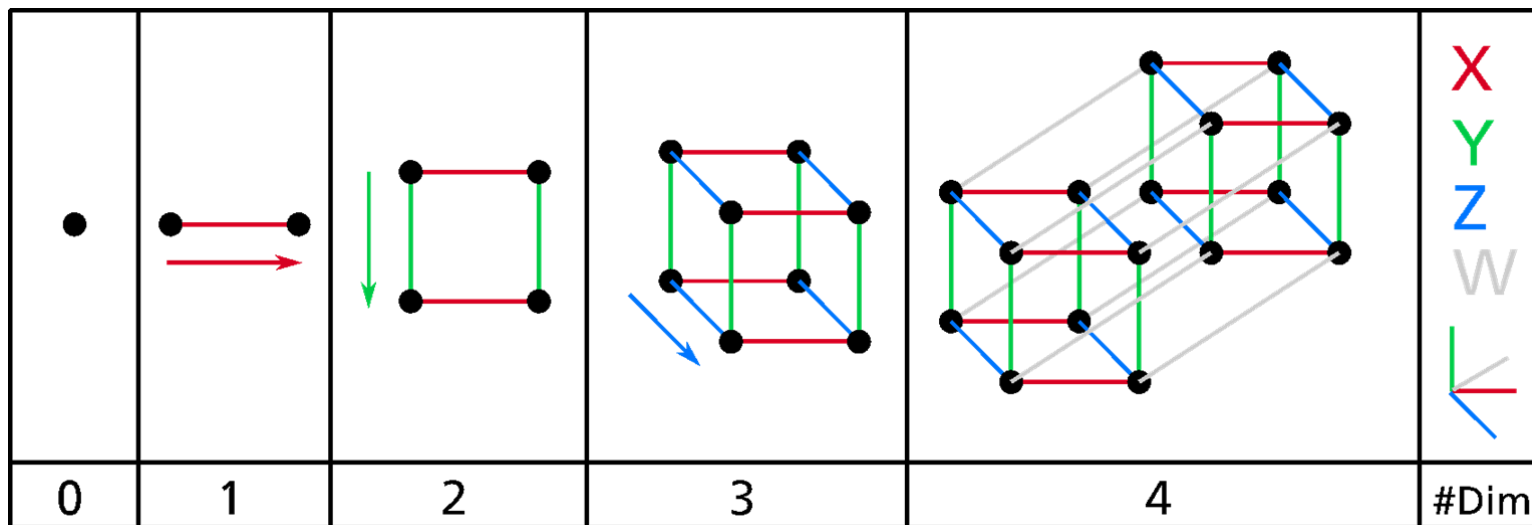


Conclusion #2

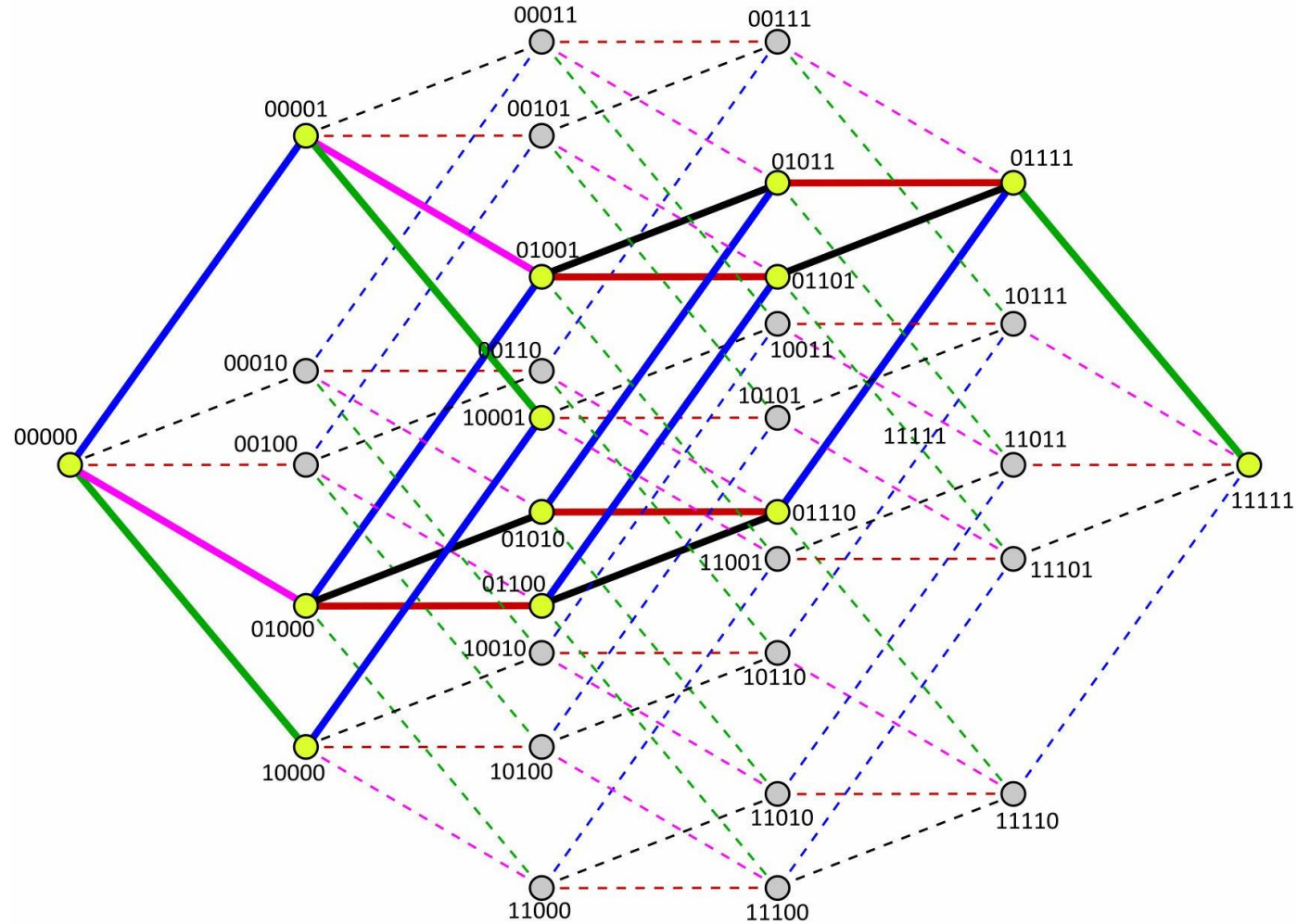
- ✓ Just 15% of amino acids found in yeast His3 orthologues were always neutral;
- ✓ The impact on fitness of the remaining 85% depended on the genetic background;
- ✓ Furthermore, at 67% of sites, amino acid replacements were under sign epistasis, having both strongly positive and negative effect in different genetic backgrounds;
- ✓ 46% of sites were under reciprocal sign epistasis.

How to find all hypocubes in random mutagenesis experimental data?

Creation of hypercubes

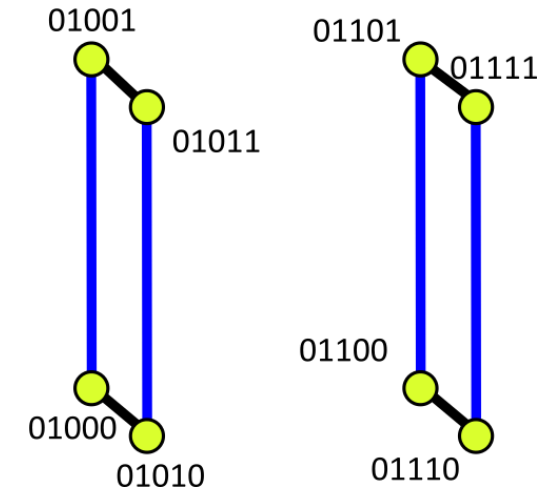
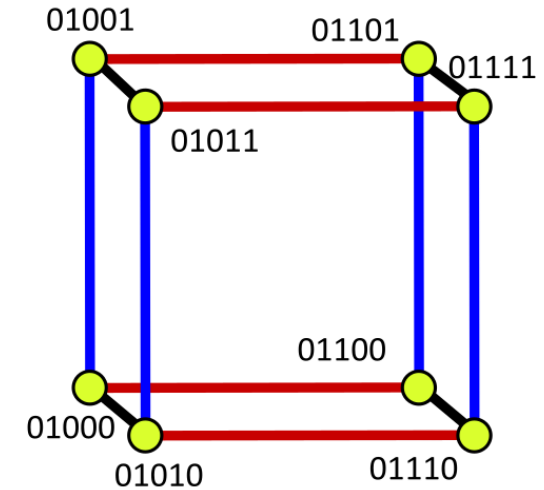


Finding all hypercubes



Idea for the algorithm

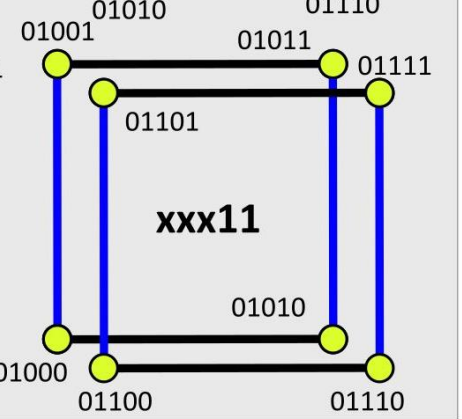
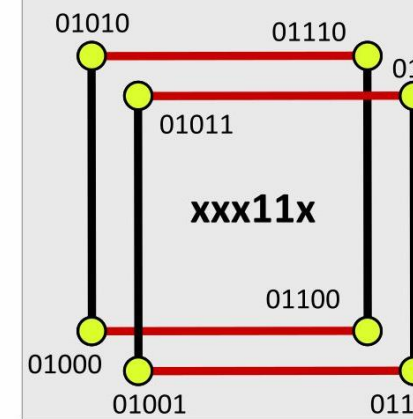
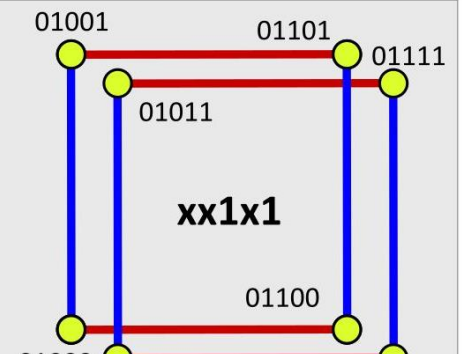
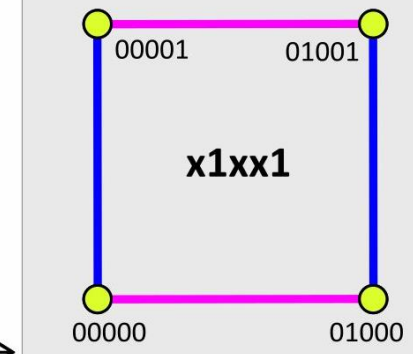
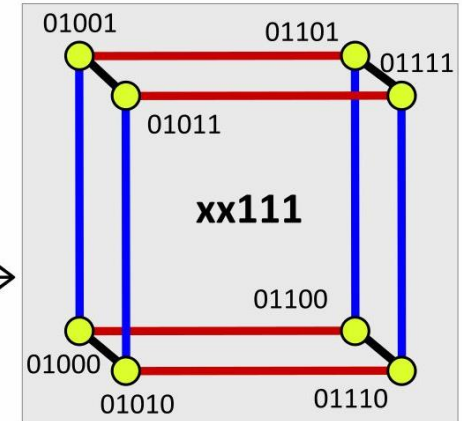
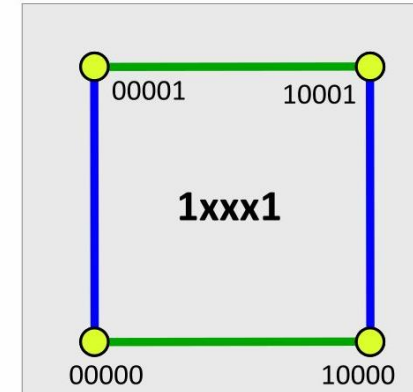
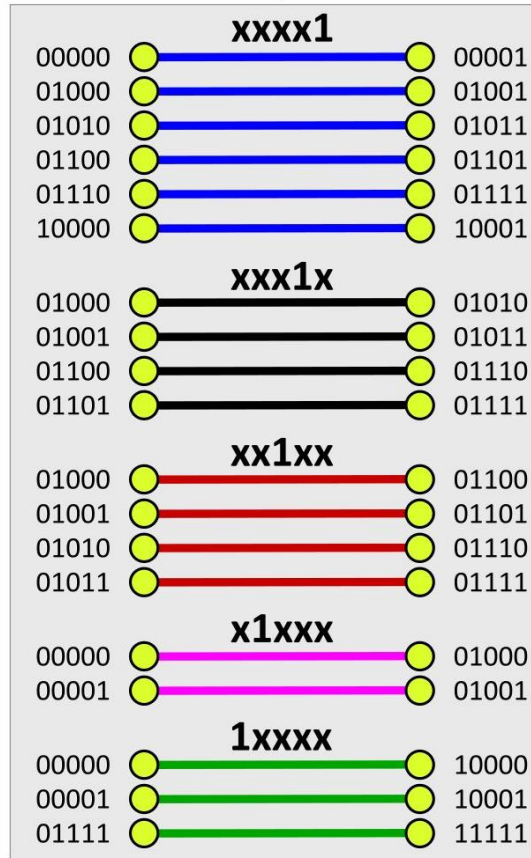
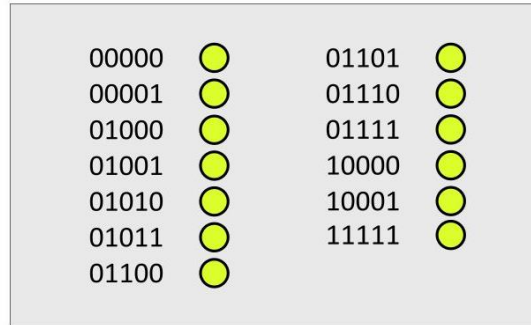
- We use the fact that N-dimensional hypercube consists of two parallel (N-1)-dimensional hypercubes



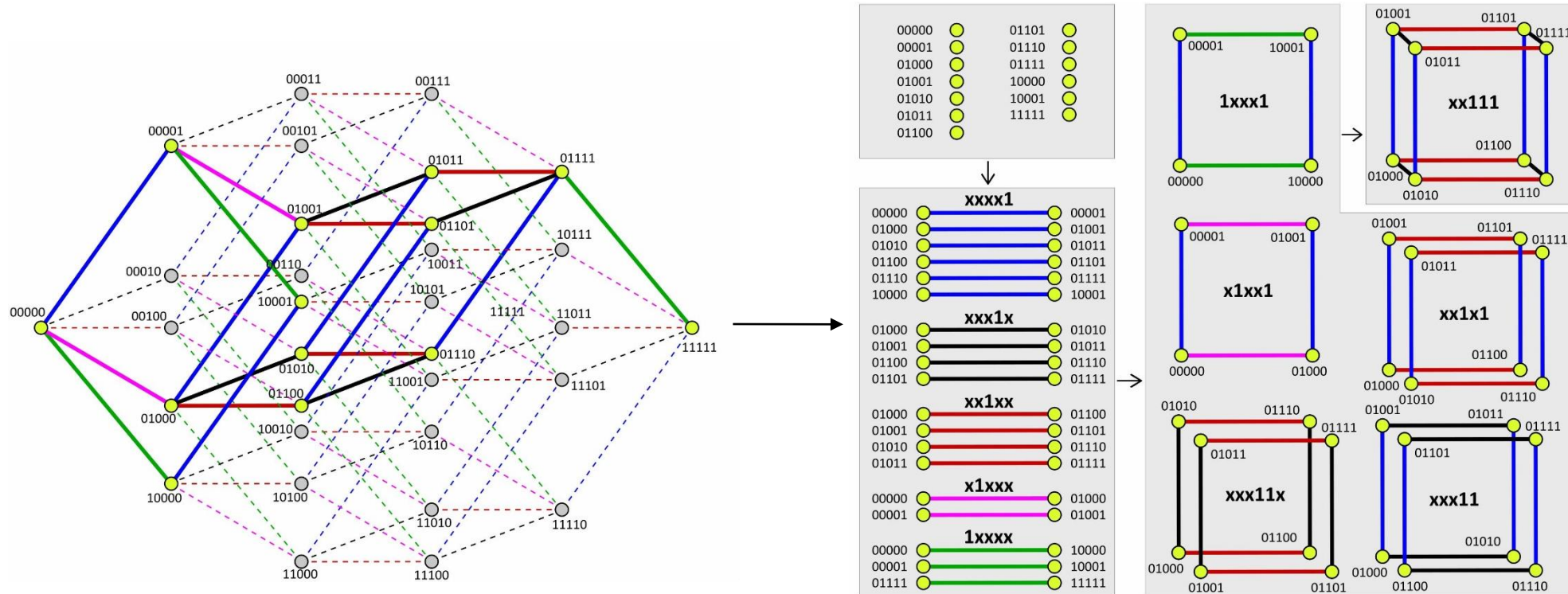
Algorithm

Bioinformatics, accepted

<https://github.com/ivankovlab/HypercubeME>



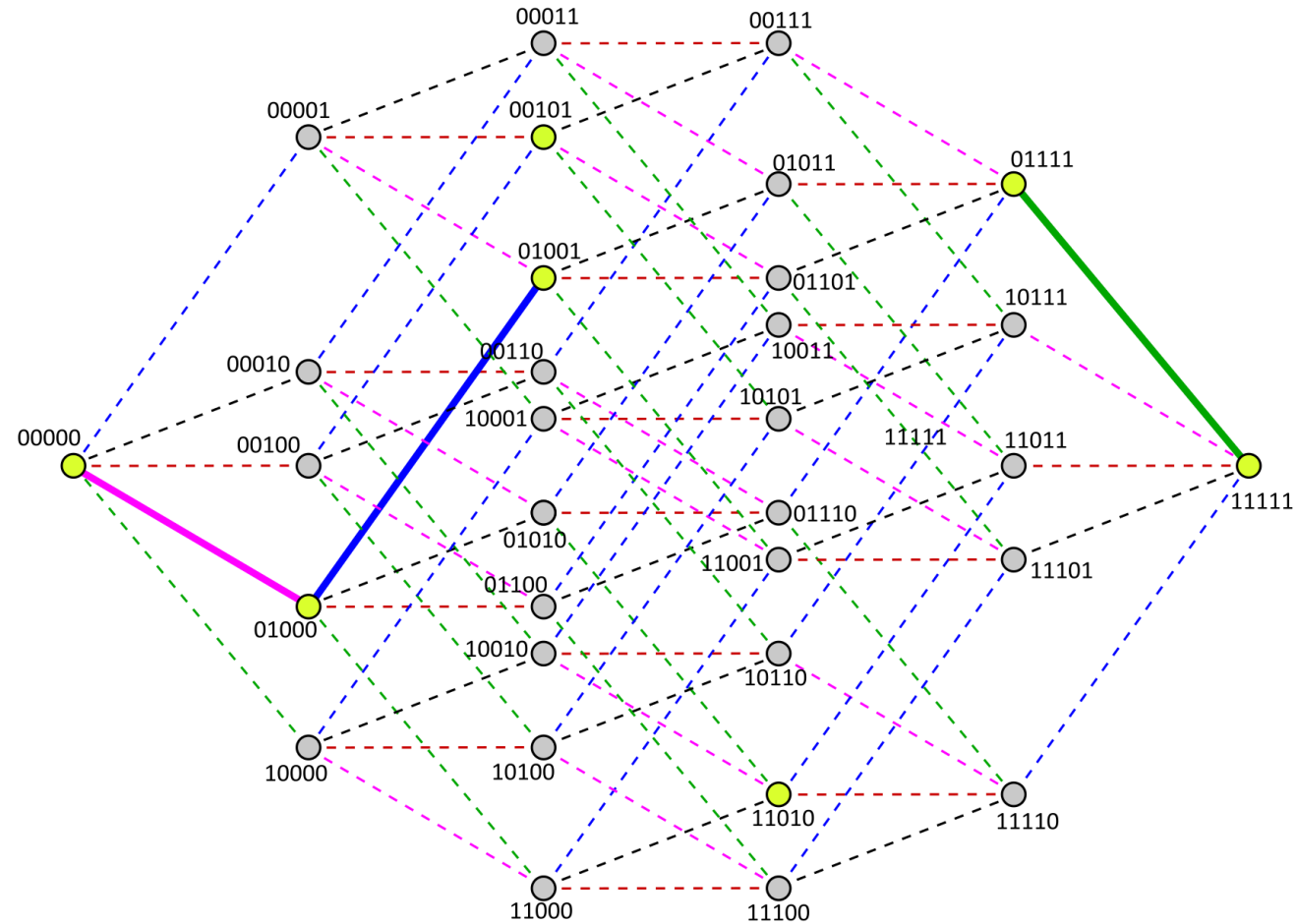
Application to HIS3 data



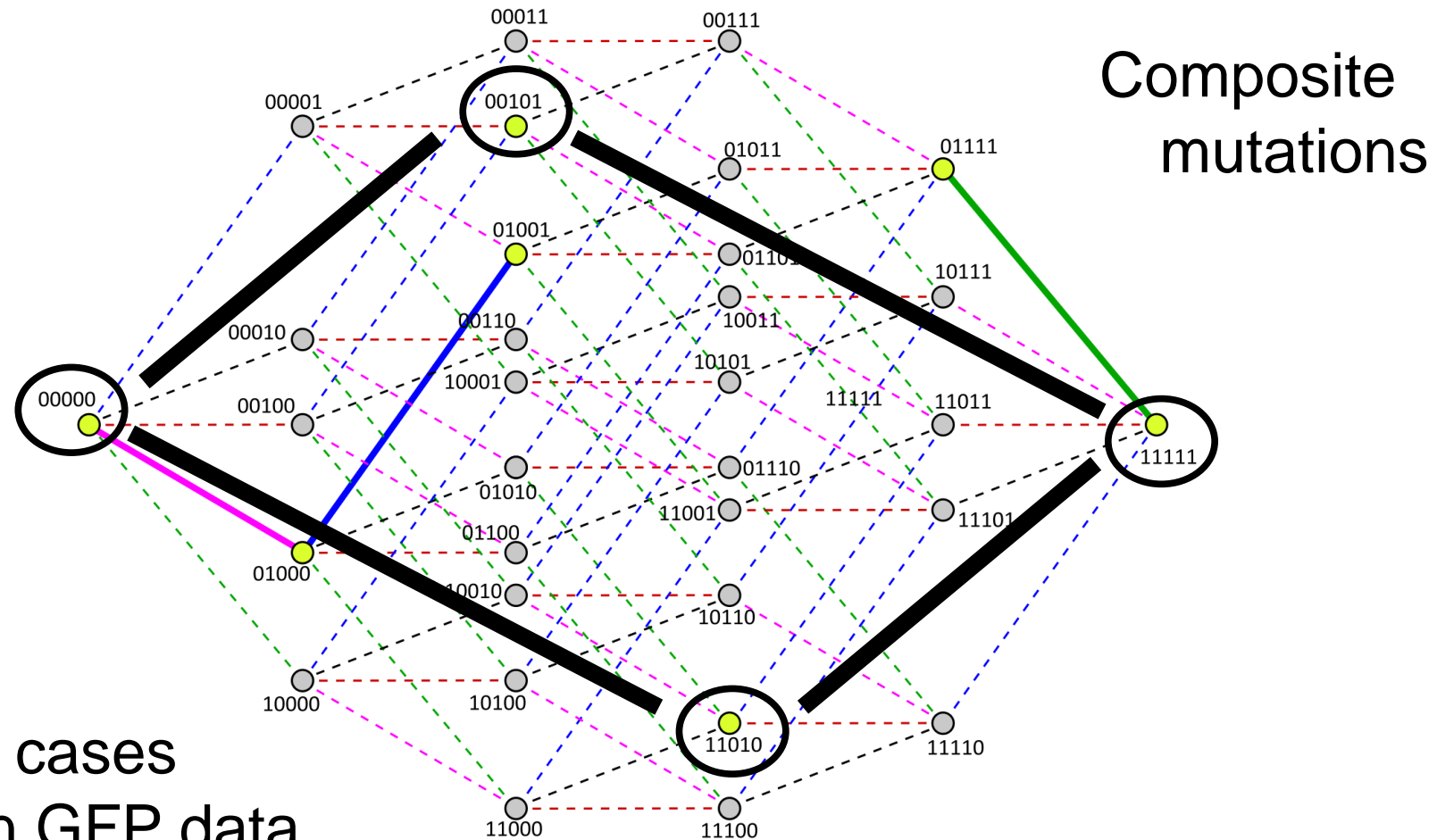
- All 199,847,053 hypercubes were found in the data from HIS3 experiment (Pokusaeva et al., 2019)
- 88% of them are of order 3 and higher

Can we study epistasis on sparse data?

Example of sparse data



Rectangles in genotype space



Uni- vs. multi-dimensional epistasis

Issue

In GFP data 6% of variance was due to multi-dimensional epistasis

However, sign and reciprocal sign cases found were rare and did not explain that variance.

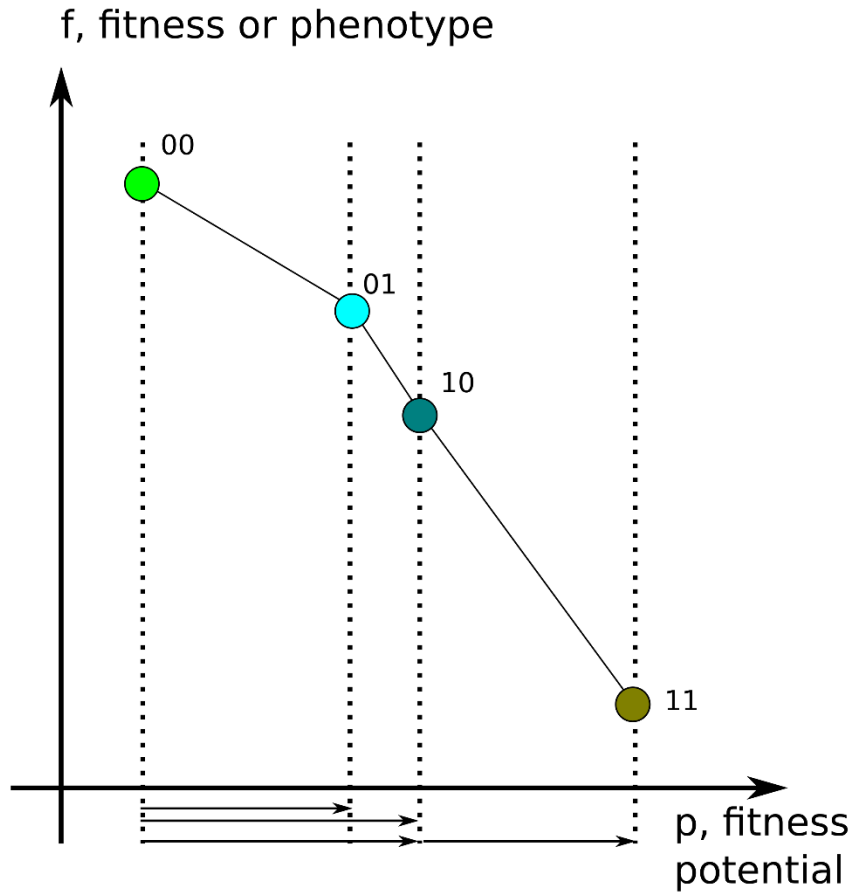
Issue

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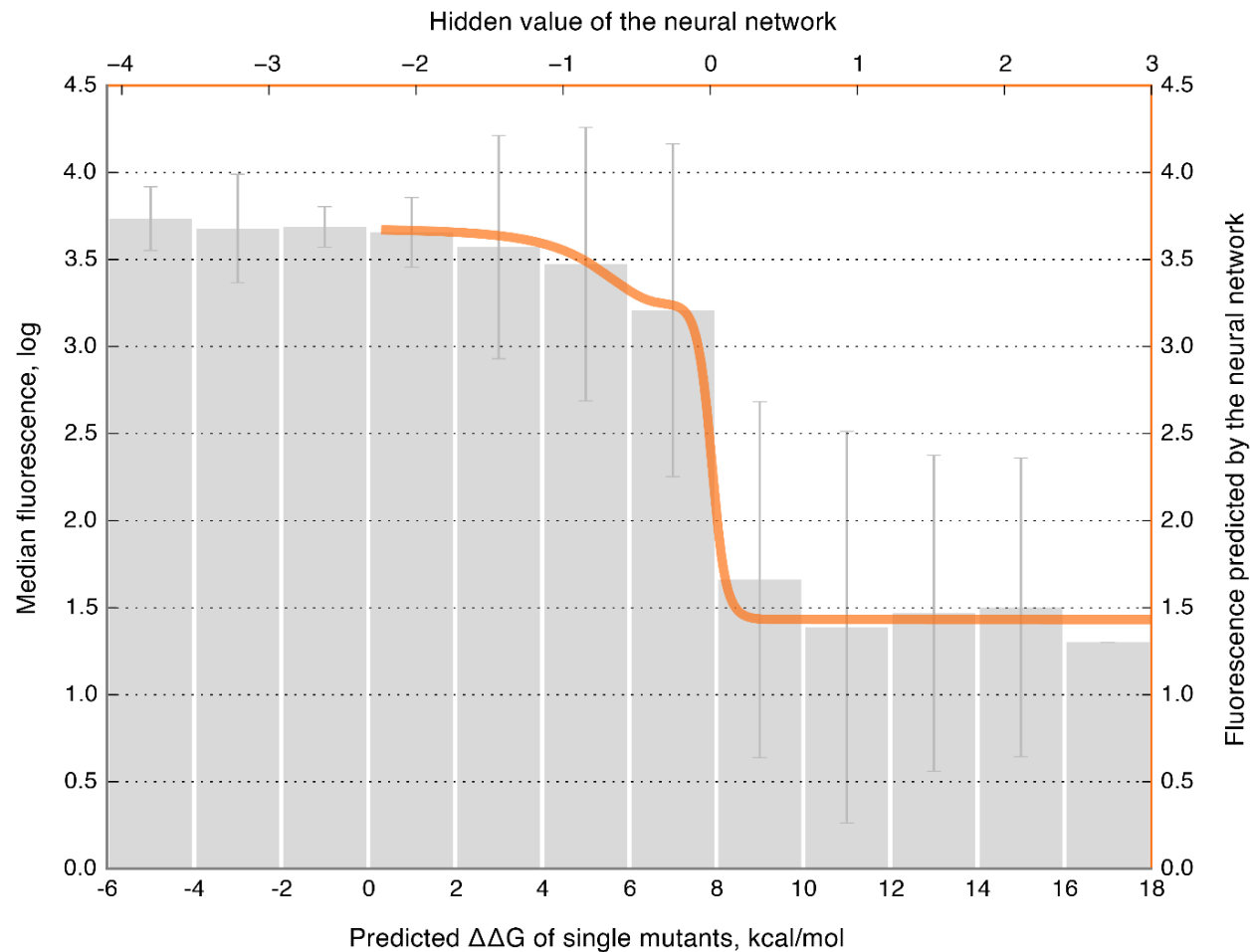
Are there other types of multi-dimensional epistasis?

Fitness potential concept



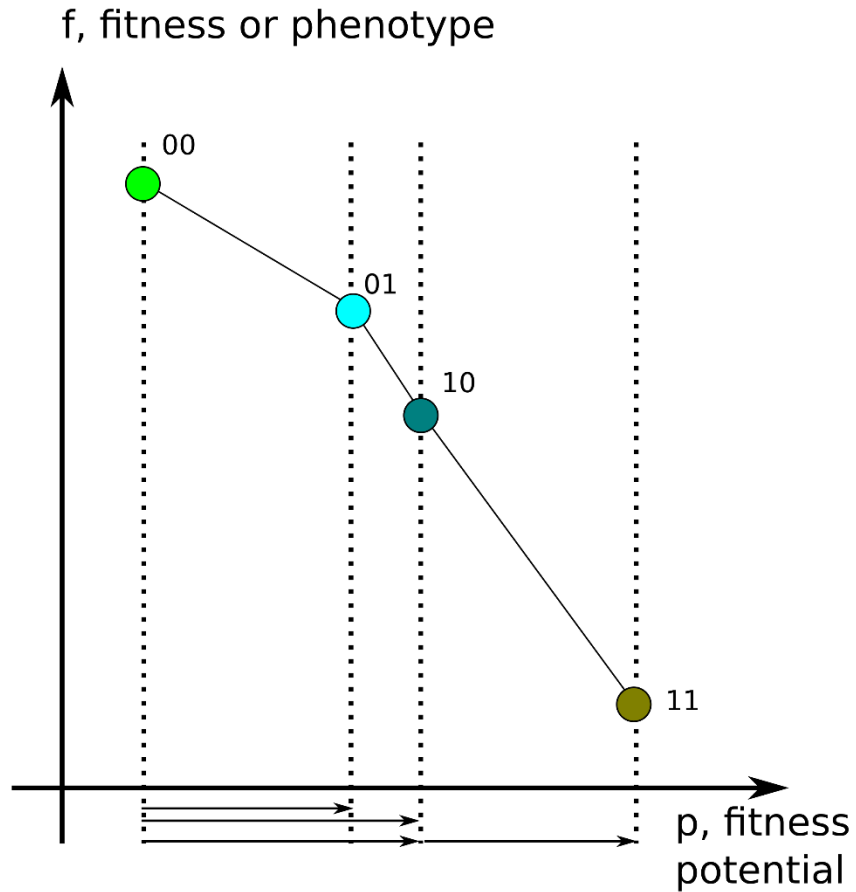
$$p(g) = const + \sum_{i=1} \alpha_i \delta_i$$

Protein stability – fitness potential?



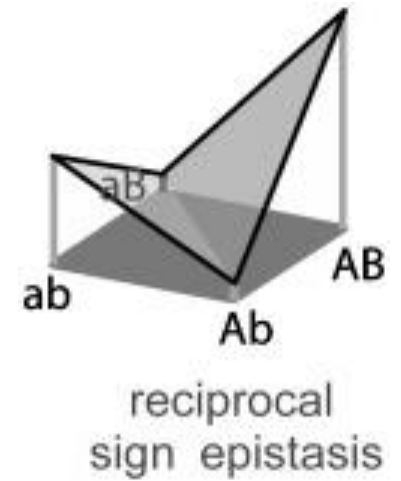
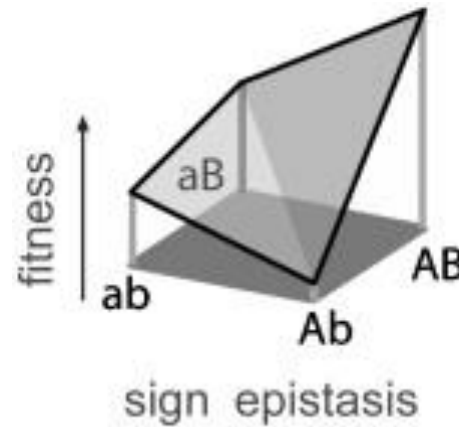
MDE cases

Uni-

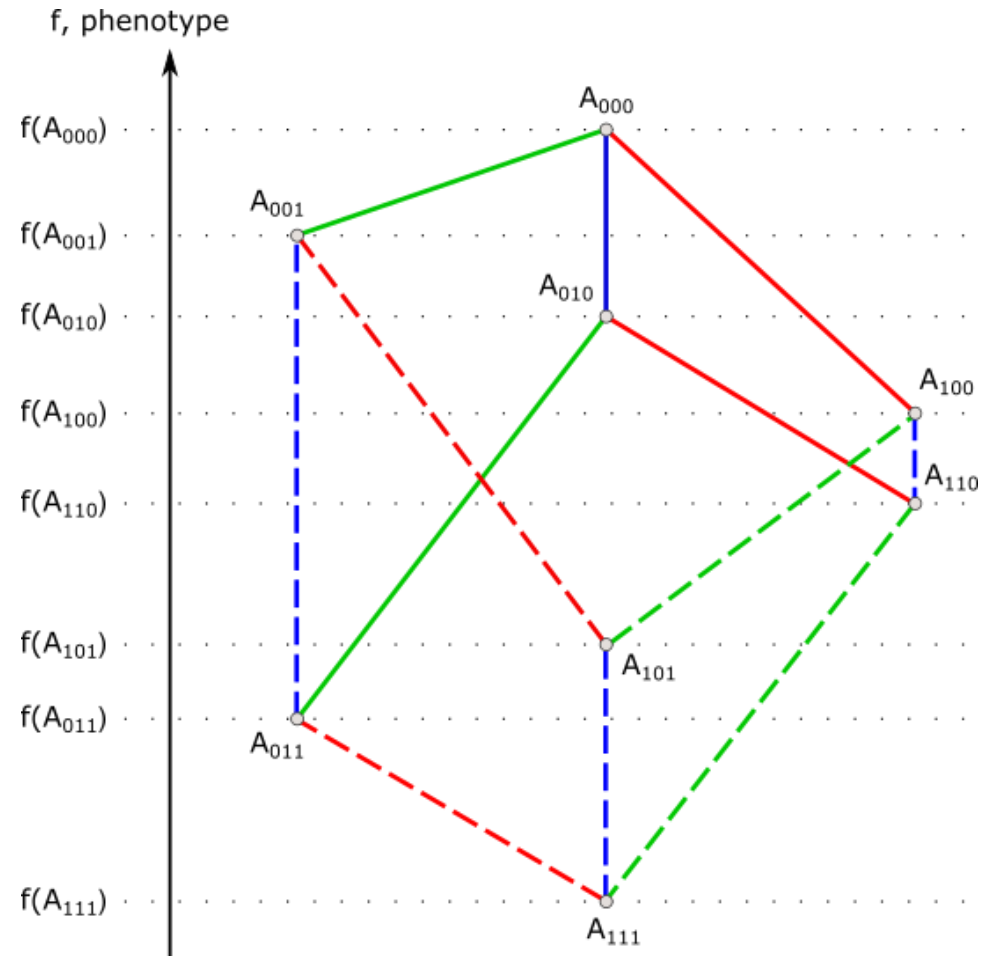


$$p(g) = const + \sum_{i=1} \alpha_i \delta_i$$

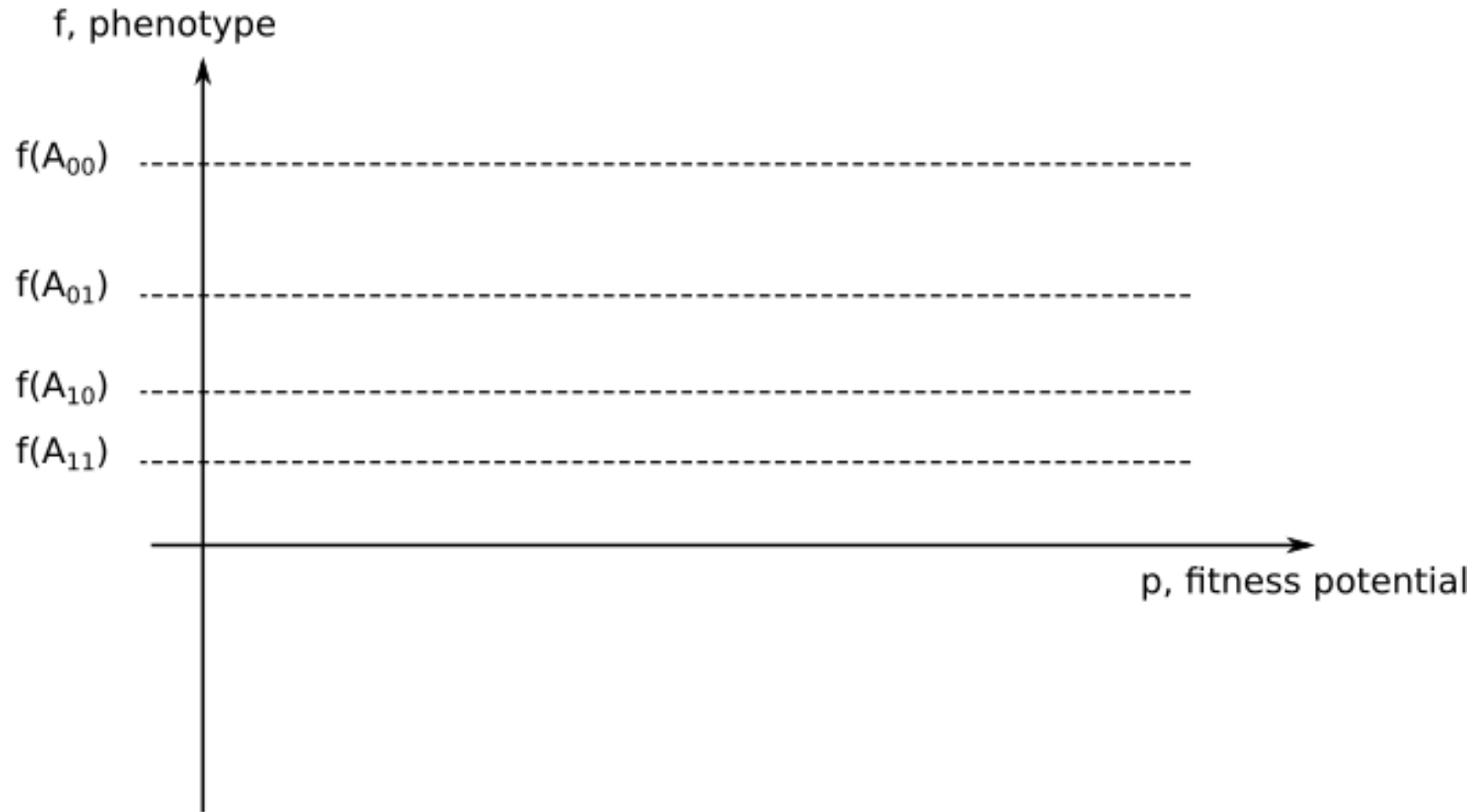
Multi-dimensional epistasis



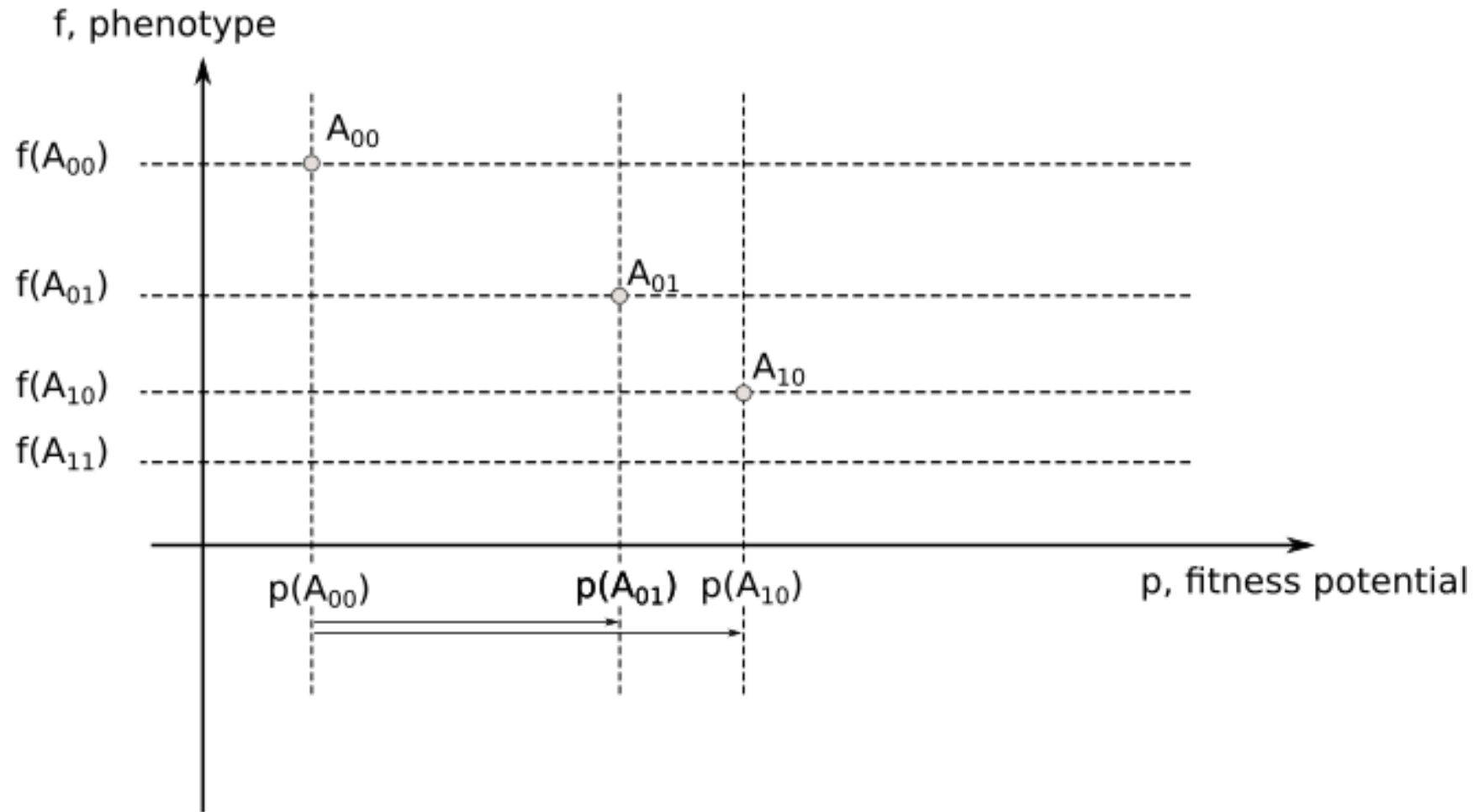
New type of MDE



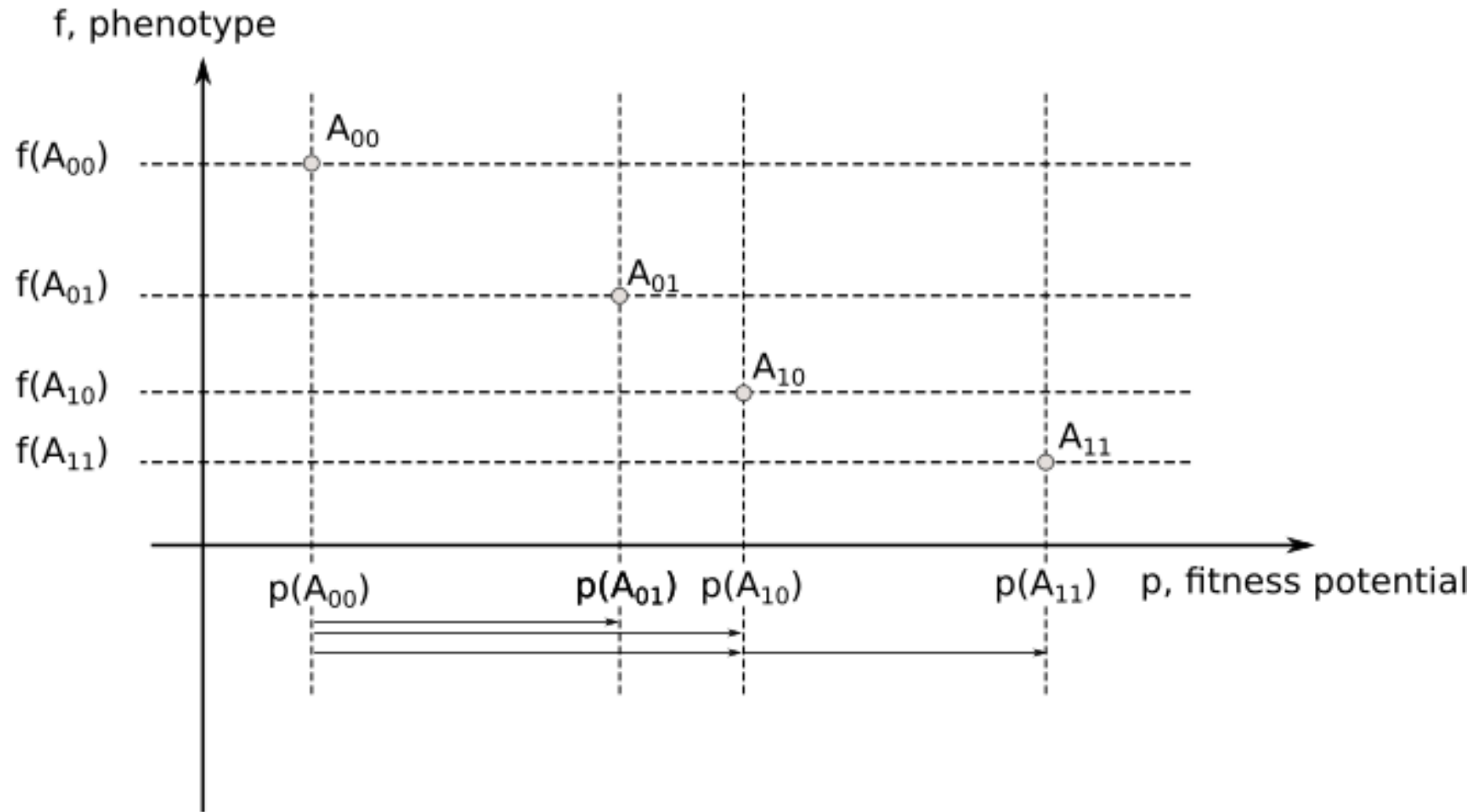
Another example of new MDE



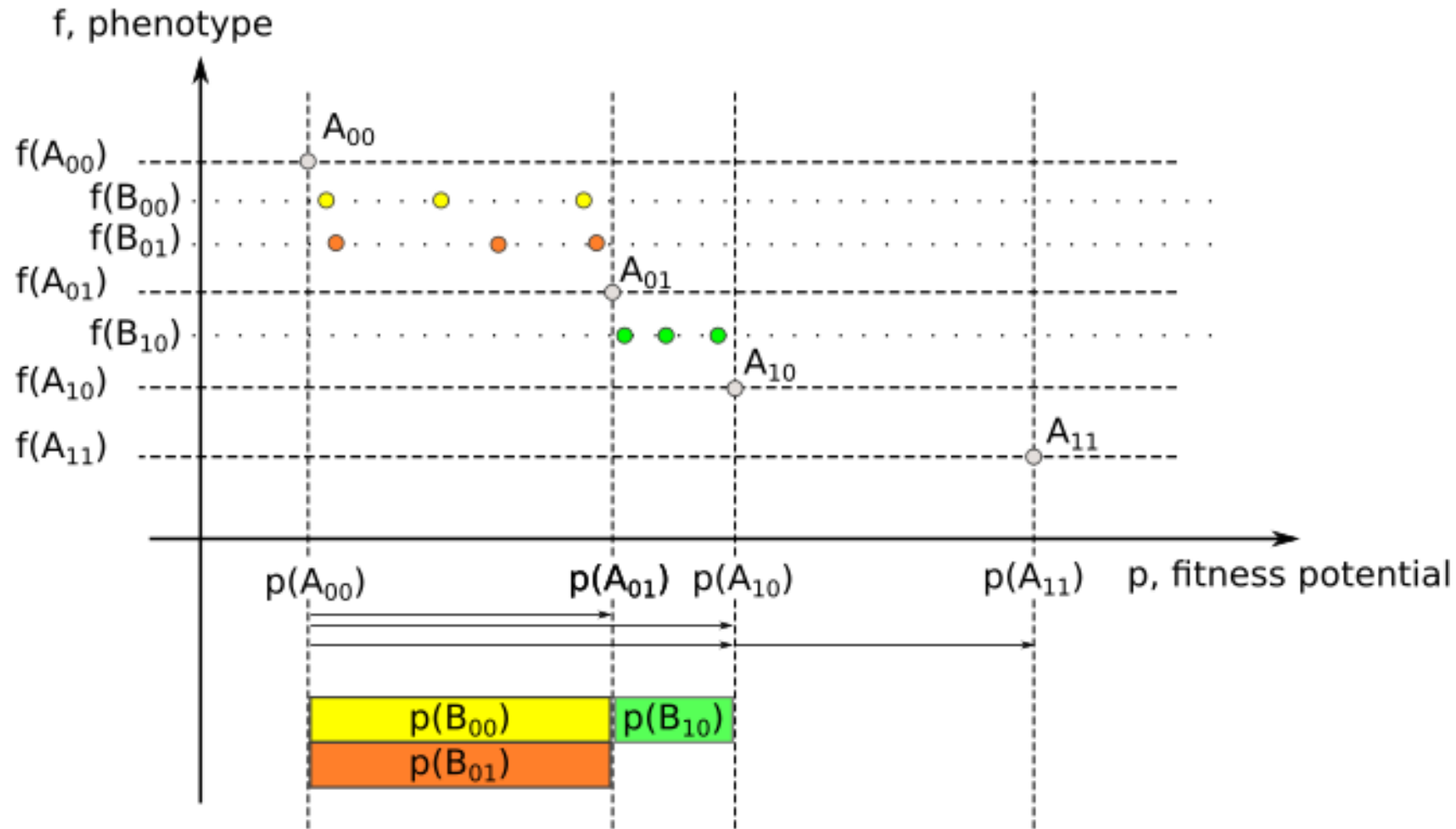
Another example of new MDE



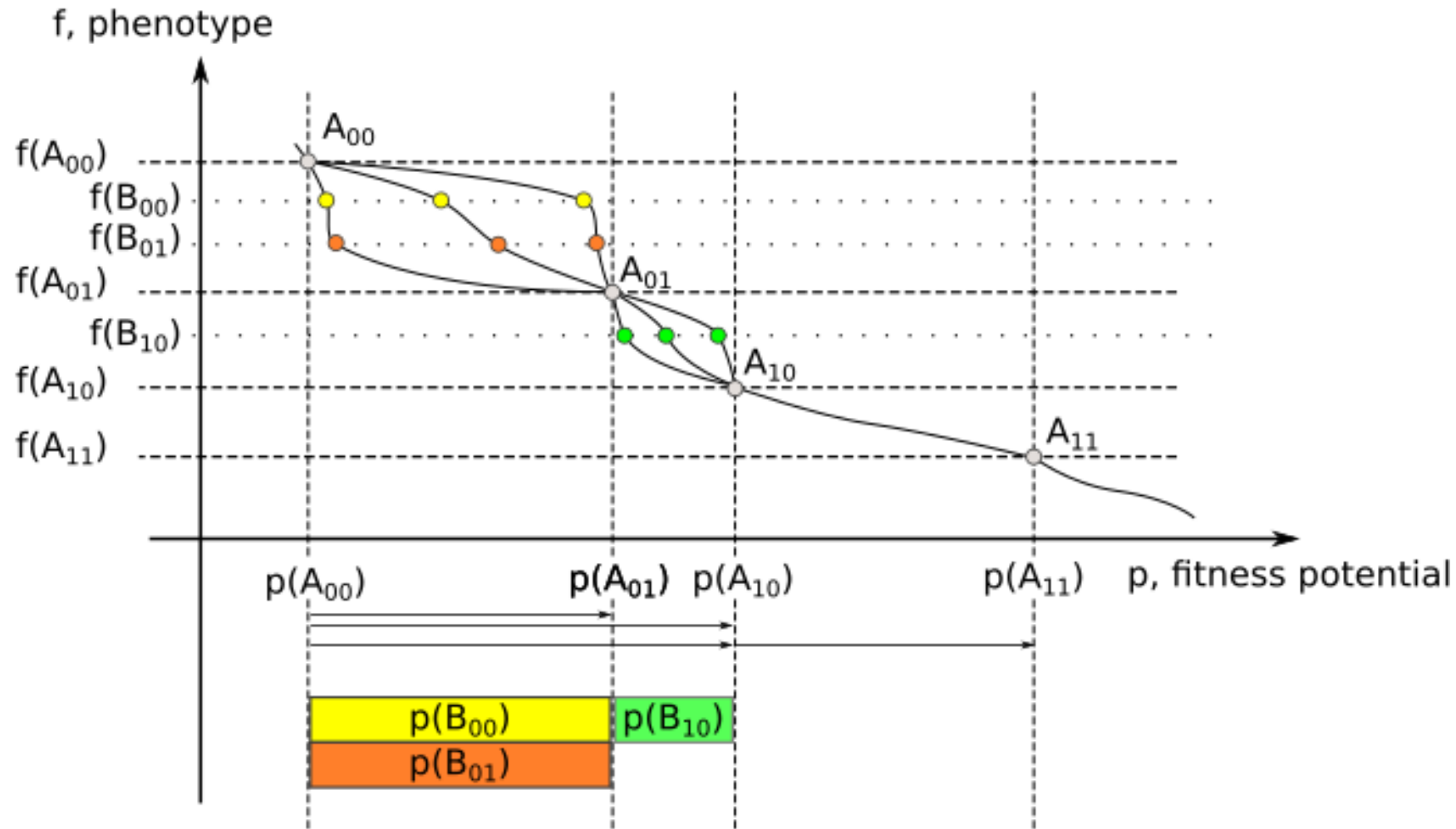
Another example of new MDE



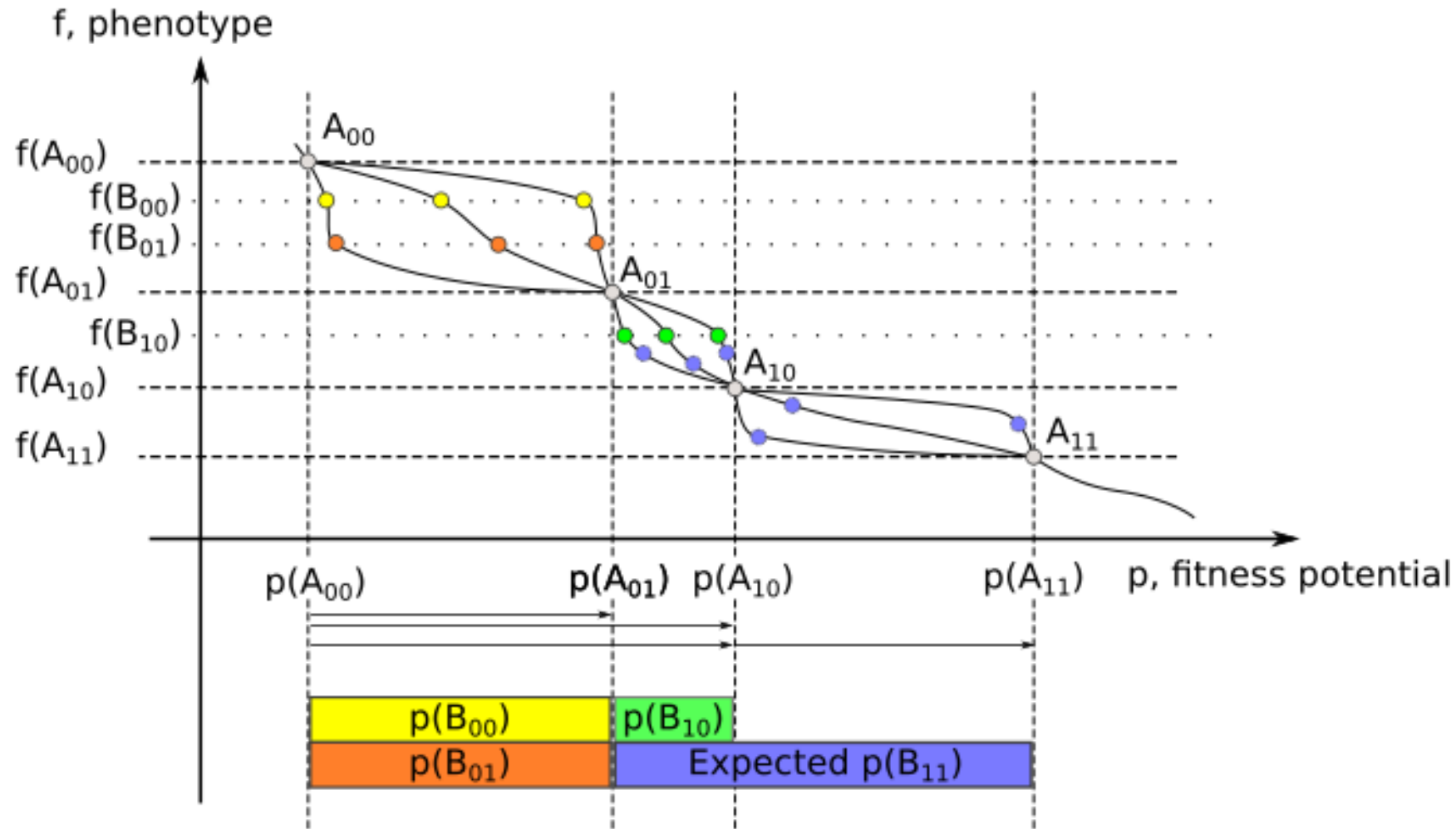
Another example of new MDE



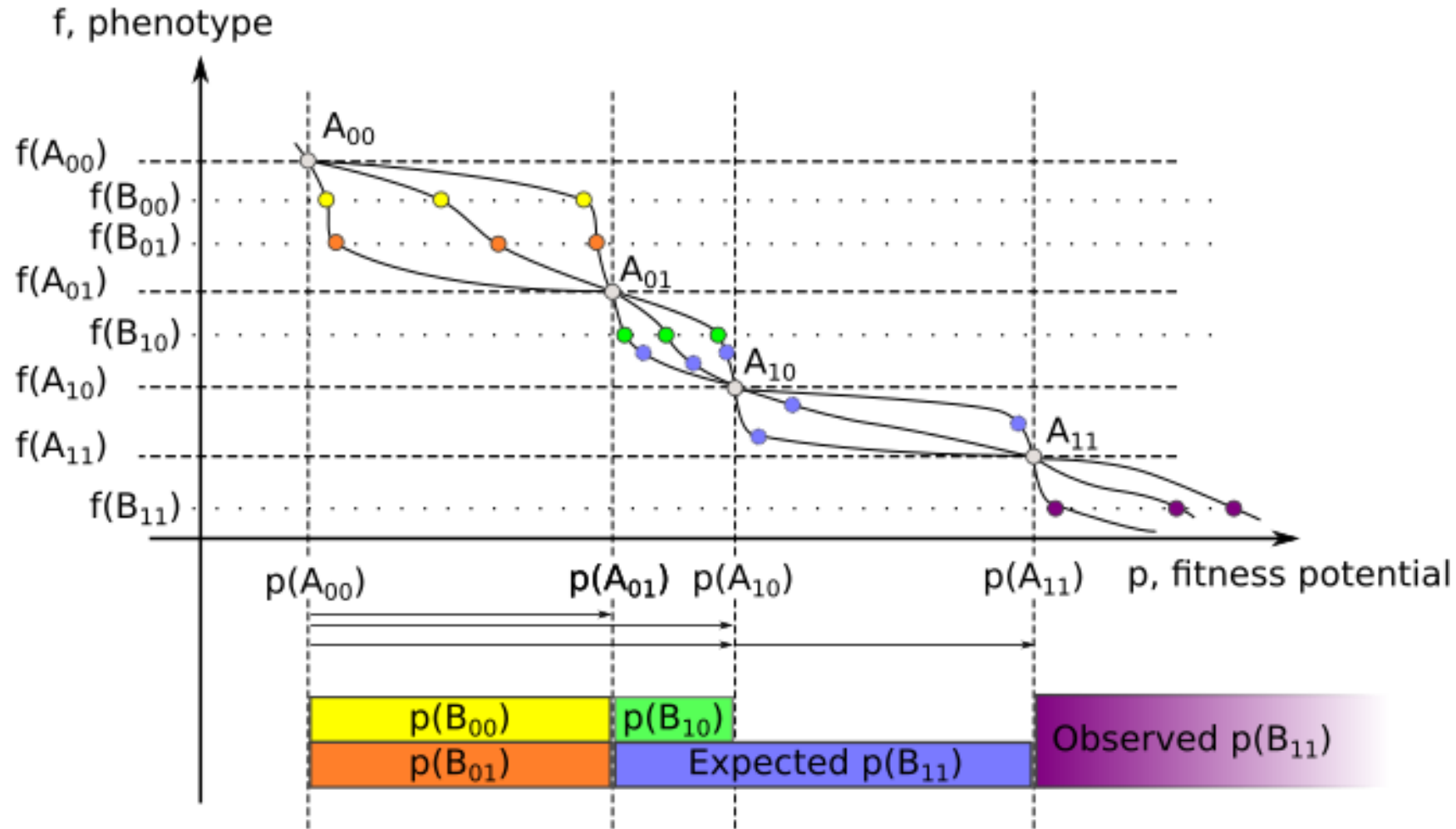
Another example of new MDE



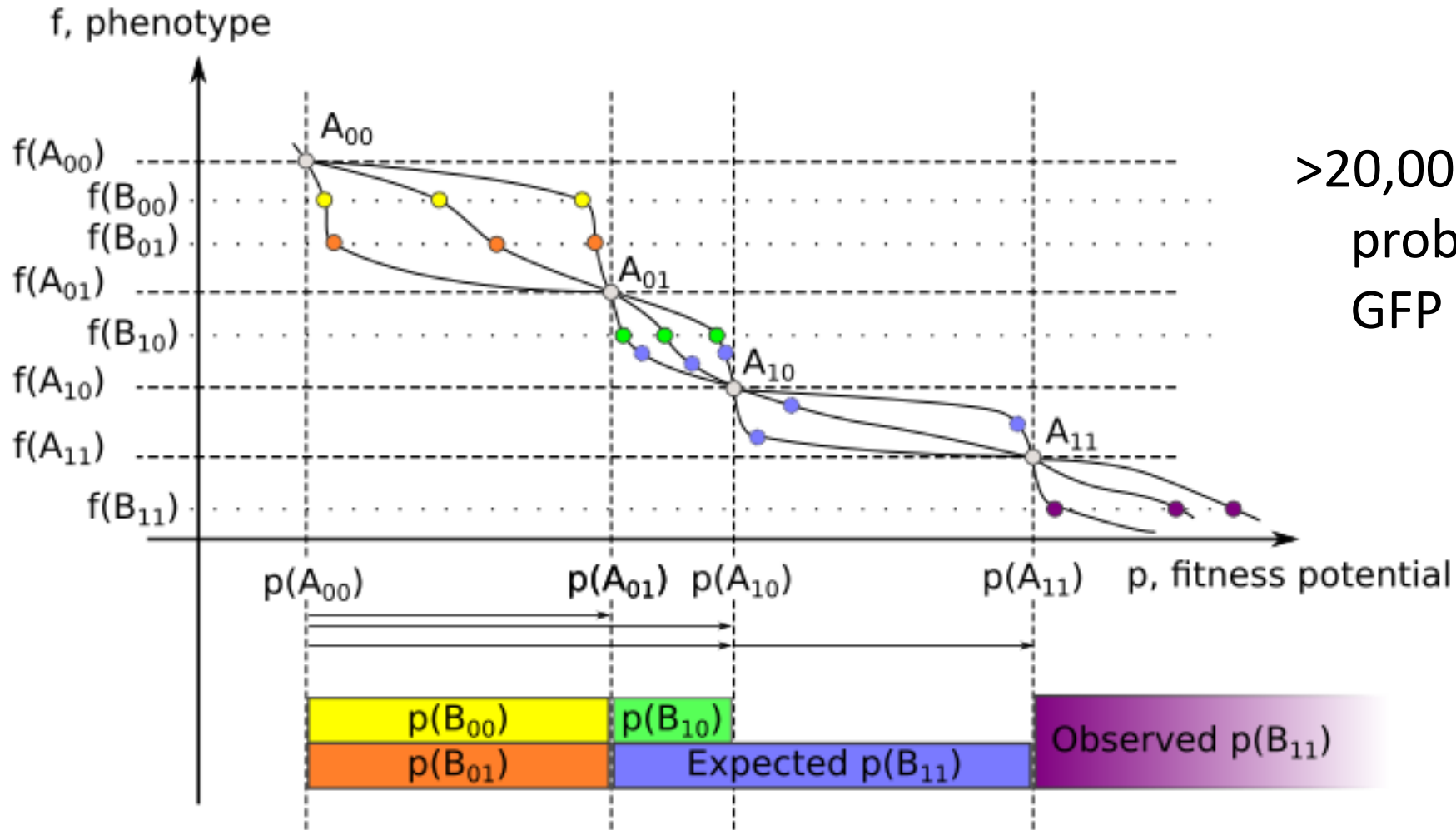
Another example of new MDE



Another example of new MDE



Another example of new MDE

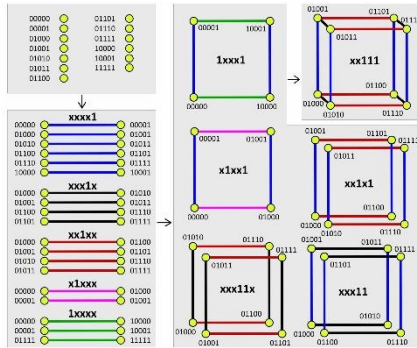


>20,000 cases with probability >95% in GFP data

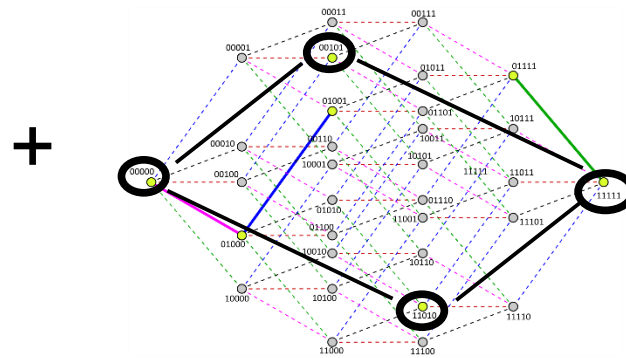
Hyperrectangles

Further tool development for finding epistasis:

Hypercubes



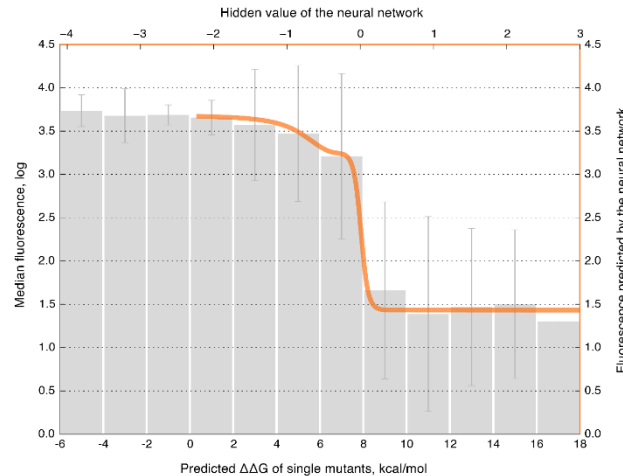
Composite mutations



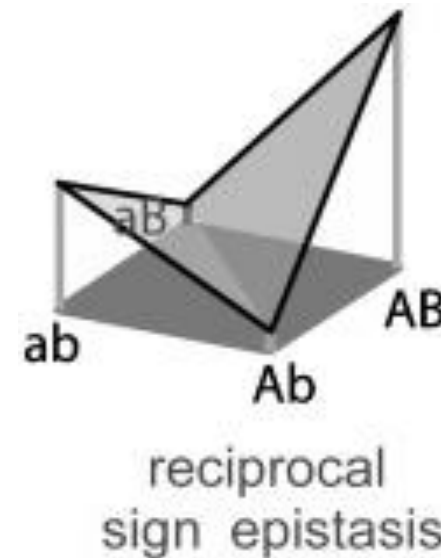
= Hyperrectangles

Relationship between HOE & MDE

Higher-order but not multi-dimensional



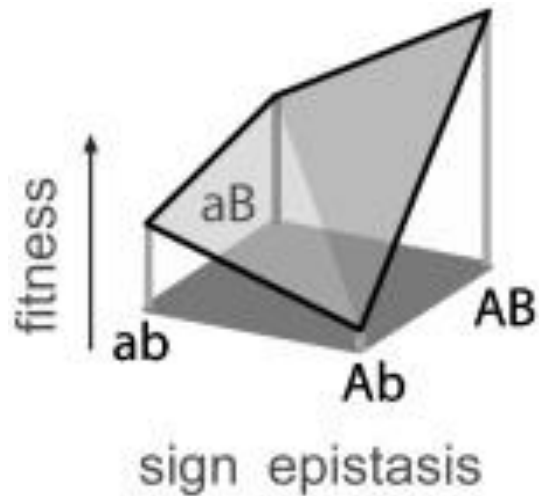
Multi-dimensional but not higher-order



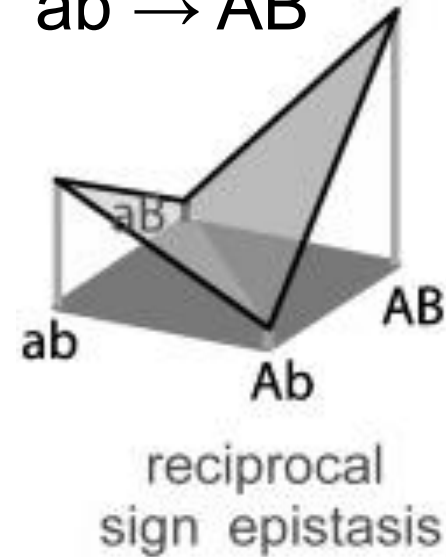
Is it true that higher-order epistasis results from non-linearity while multi-dimensional results from physical interactions?

Pathway accessibility and MDE

Two-dimensional:
50% of pathways
 $ab \rightarrow AB$



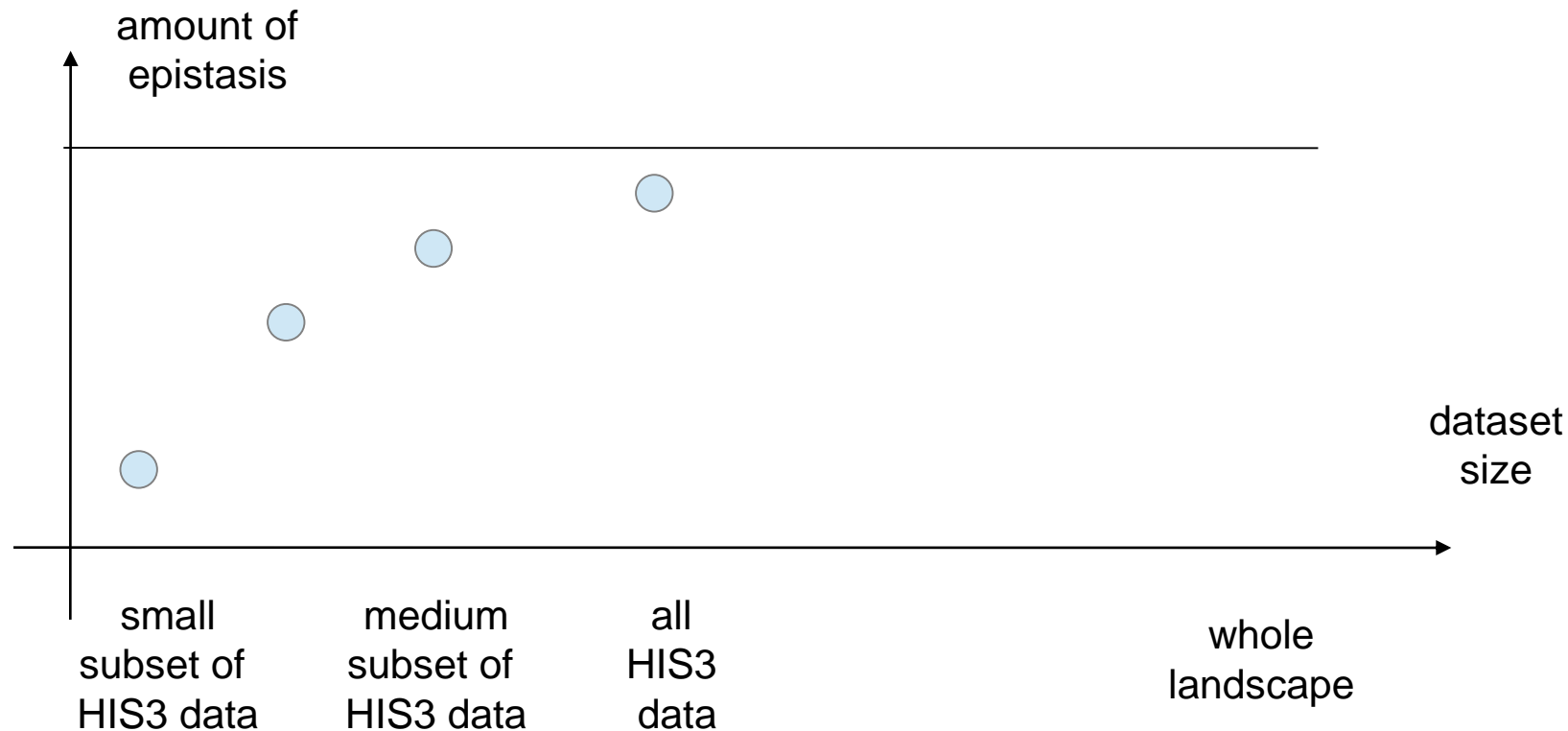
Two-dimensional:
0% of pathways
 $ab \rightarrow AB$



- ✓ New type of multi-dimensional epistasis: from 0% to 100%
- ✓ Correlation on experimental data?

Extrapolation of epistasis

Find epistasis for fitness landscape subsets of different sizes and extrapolate. Can we find a limit?



Acknowledgements

Grigoriy Leleytner

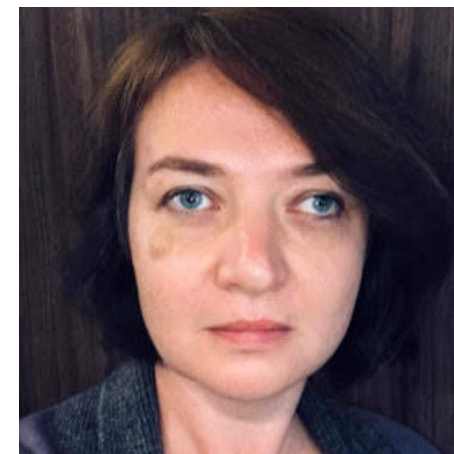


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